

1 **Towards imaging flow at the base of the mantle with**
2 **seismic, mineral physics and geodynamic constraints**

3 **Andy Nowacki¹ and Sanne Cottaar²**

4 ¹School of Earth and Environment, University of Leeds, UK

5 ²Department of Earth Sciences, University of Cambridge, UK

6 **Abstract**

7 Perhaps the least ambiguous signal that the mantle is convecting comes from observa-
8 tions of seismic anisotropy—the variation of wave speed with direction—which must arise
9 due to the ordering of material as deformation occurs. Therefore significant effort has
10 been made over many years to infer the direction and nature of mantle flow from these
11 data. Observations have focussed on the boundary layers of the mantle, where deforma-
12 tion is expected to be strongest and where anisotropy is usually present. While prospects
13 for mapping flow seem good, the lack of knowledge of several key issues currently holds
14 progress back. These include the cause of anisotropy in the lowermost mantle, the causative
15 material’s response to shear, and the single-crystal or -phase seismic properties of the
16 causative materials. In this chapter we review recent observations of lowermost mantle
17 anisotropy, constraints on mineral elasticity and deformation mechanisms, and challenges
18 in linking geodynamic modelling with seismic observations.

19 **1 Introduction**

20 Seismic anisotropy, i.e. the variation of seismic velocity with propagation direction
21 and polarisation, is observed in a number of regions within the Earth. The strength of
22 anisotropy is particularly strong in the crust, at the top and the bottom of the mantle,
23 and in the inner core (Mainprice, 2007). In the upper mantle, observed seismic anisotropy
24 has been used to map asthenospheric flows (Becker and Lebedev, this volume) and un-
25 derstand slab dynamics (Huang and Zhao, this volume). In the lowermost mantle, un-
26 derstanding anisotropy in terms of flow is more elusive, as seismic observations are sparse,
27 and mineral physical constraints more uncertain. The dynamics of the lowermost man-
28 tle are of particular interest, as they reflect the lower thermal and mechanical bound-
29 ary layer of the convecting mantle. Mapping flow directions in this region would signif-
30 icantly help our understanding of the role of this boundary in mantle dynamics, and more
31 specifically the role of the large low-shear velocity provinces (‘LLSVPs’) (Rudolph et al.,
32 this volume).

33 Albeit challenging, significant efforts have been made to use seismic anisotropy to
34 understand the underlying crystal preferred orientations (CPO) and flow directions (e.g.,
35 Karato, 1998). This is based on the assumption that flow, and the internal crystallographic
36 deformation mechanisms that accommodate the flow, cause alignment of intrinsically anisotropic
37 crystals. This chapter offers a condensed review of seismic observations and mineral phys-

38 ical and geodynamical constraints on seismic anisotropy, and for a more in-depth review
 39 we refer to Nowacki et al. (2011) and Romanowicz & Wenk (2017). Here, we focus on
 40 the endeavours, mainly over the last decade, to tie these disciplines together and map
 41 flow directions in the lowermost mantle, and the specific challenges posed when compar-
 42 ing these results to seismic observations.

43 **2 Observational constraints on lowermost mantle flow**

44 **2.1 Global tomographic models**

45 A number of tomographic modellers invert for seismic anisotropy in the lowermost
 46 mantle. Inverting the full anisotropic elastic tensor (i.e., all 21 parameters) is unfeasi-
 47 ble. The only component of anisotropy generally inverted for in the lowermost mantle
 48 is the velocity difference between horizontally polarised shear velocity, V_{SH} , and verti-
 49 cally polarised shear velocity, V_{SV} . This component of anisotropy is named radial anisotropy
 50 (or vertically transverse isotropy) and the degree of anisotropy can be expressed by the
 51 value $\xi = V_{SH}^2/V_{SV}^2 = C_{66}/C_{44}$, where C is the Voigt matrix representation of elas-
 52 ticity and the 3-axis is vertical.

53 For the upper mantle, radial anisotropy is well constrained due to the unique sen-
 54 sitivities of the two types of surfaces waves (Becker and Lebedev, this volume). For the
 55 lower mantle, one or both of normal modes and body waves must be used. Normal mode
 56 inversions for 1D radial models show no significant component of ξ (Beghein et al., 2006;
 57 de Wit & Trampert, 2015). 3D tomographic models show a mainly isotropic lower man-
 58 tle with lateral variations in ξ on the order of 0.97–1.03 in the lowermost mantle (e.g.,
 59 Moulik & Ekstrom, 2014; Auer et al., 2014; Chang et al., 2015; French & Romanowicz,
 60 2015). There are strong differences between these models, some of which can be attributed
 61 to their treatment of the crust in the inversion, which is shown to affect the radial anisotropic
 62 signature of the lowermost mantle (Ferreira et al., 2010; Panning et al., 2010). In gen-
 63 eral, a geographical trend emerges where $\xi > 1$ (equivalently, $V_{SH} > V_{SV}$) in regions
 64 with fast shear wave velocity interpreted to be slab graveyards, and opposite signature
 65 of $\xi < 1$ is seen in regions of slow shear wave velocity, i.e. the LLSVPs. In Figure 1 this
 66 relationship is illustrated with histograms of ξ values for the fast and slow regions as in-
 67 terpreted by Cottaar & Lekić (2016), as well as a vote map of ξ values, which at each
 68 point at 2800 km depth shows the count of all tomography models which have a value

69 of ξ above or below 1. While all models show a significant shift in their histograms for
 70 the fast and slow region, the shifts between their mean values is small, with the largest
 71 shift of 1.1% in SEMUCBwm1, and the smallest shift of 0.38% in SAVANI. The vote map
 72 also suggests a relationship between dV_S and ξ . Interpreting this general trend should
 73 be done with caution as any relationship between dV_S and ξ could be an artefact of the
 74 inversion, specifically the negative ξ values appear prone to be leakage of the slow isotropic
 75 velocities (Chang et al., 2015). One thing that is interesting to note from the vote map
 76 is the smaller slow shear region beneath the Ural mountains, dubbed the Perm anomaly
 77 (Lekić et al., 2012), does not correlate directly with a signal of $\xi < 1$, but a small anomaly
 78 showing $\xi < 1$ appears offset to the south.

79 Studies are even more limited in constraining P wave radial anisotropy ($\phi = V_{PV}^2/V_{PH}^2 =$
 80 C_{33}/C_{11}). Global studies constraining 1D radial P wave anisotropy show no agreement
 81 in the likely signature (Beghein et al., 2006; de Wit & Trampert, 2015). Global 3D stud-
 82 ies have often applied an assumed scaling between the S and P wave anisotropy as a start-
 83 ing model. When they do include P wave radial anisotropy independently (Soldati et al.,
 84 2003; Tesoniero et al., 2016), they judge their results not to be robust. Inversions using
 85 body waves are heavily under-constrained (Boschi & Dziewoński, 2000). The synthetic
 86 study of P. J. Koelemeijer et al. (2012) shows general sensitivity of normal modes to P
 87 wave anisotropy, although it also predicts it is sensitive to trade-offs.

88 A potential way forward for global studies lies in the understanding of a third anisotropic
 89 parameter, $\eta = C_{13}/(C_{11} - 2C_{44})$, which is related to the S and P velocities at inter-
 90 mediate incidence angles. de Wit & Trampert (2015) show that this parameter has a ro-
 91 bust 1D signature of $\eta < 1$ across the lower 1000 km of the mantle. Kawakatsu (2015)
 92 suggests a rewrite of η for a more physical relationship with wave incidence angle, and
 93 shows that constraining this parameter, η_κ , can help resolve whether horizontally isotropic
 94 layers could cause the observed anisotropy.

104 **2.2 Regional body wave observations**

105 Locally, deep mantle seismic anisotropy can be observed through shear wave split-
 106 ting of body waves. One of the main challenges is to determine the relative contribution
 107 to splitting from the uppermost and lowermost mantle, and whilst often assuming the
 108 rest of the lower mantle is isotropic. A general approach is to use two seismic phases with

109 comparable ray paths across the upper mantle, while one reference phase has a differ-
 110 ent or no ray path across the lowermost mantle. Ideally the reference phase shows no
 111 or minimal splitting and all splitting in the other phase can be attributed to the low-
 112 ermost mantle. Otherwise corrections for splitting from the upper mantle need to be ap-
 113 plied to attribute splitting to the lower mantle (e.g., Wookey et al., 2005).

114 One potential set consists of the ScS and S phases (Figure 2). For the distance range
 115 of 60–85°, the S phase turns above the lowermost mantle, while the ScS phase samples
 116 the lowermost mantle (e.g., Lay & Young, 1991; Wookey & Kendall, 2008). A second set
 117 is the SKS and SKKS phases (at epicentral distances 108–122°), for which the ray paths
 118 exit the core at different locations and converge across the mantle (e.g., Niu & Perez,
 119 2004; Wang & Wen, 2007; M. Long, 2009). SKS–SKKS pairs have the additional advan-
 120 tages over S–ScS that in an isotropic or radially-anisotropic mantle they exit the core
 121 purely polarised along the SV component, and any anisotropy along the down-going leg
 122 of the path can be ignored. Their disadvantage is that both phases can accrue splitting
 123 in the lowermost mantle and in the upper mantle. At times it is difficult to retrieve split-
 124 ting parameters and these phases are usually only used to highlight discrepant phase pairs
 125 (e.g., Deng et al., 2017).

126 Lastly, S_{diff} phases (at 100–130° distance) are compared either to S/ScS at shorter
 127 distances, or to SKKS (or SKS) at longer distances (e.g., Kendall & Silver, 1996; Vin-
 128 nik et al., 1998). The SV component of the diffracted wave attenuates much faster than
 129 the SH along the core-mantle boundary, which means S_{diff} at large distances ($>\sim 120^\circ$)
 130 becomes a purely SH polarised wave, and any splitting can be attributed to the upgo-
 131 ing leg of the ray path (Cottaar & Romanowicz, 2013).

132 In all cases, caution is required in interpreting body-wave observations if modelled
 133 using approximate methods such as ray theory, since shear waves at the base of the man-
 134 tle have a large region of finite-frequency sensitivity. For S_{diff} , travel time differences be-
 135 tween SH_{diff} and SV_{diff} can arise for purely isotropic models, especially with strong isotropic
 136 velocity gradients as one might expect due to the thermal boundary layer, due to dif-
 137 ferent finite-frequency sensitivity of the two components along the boundary (Maupin,
 138 1994; Komatitsch et al., 2010; Borgeaud et al., 2016; Parisi et al., 2018). ScS suffers to
 139 a lesser extent from finite-frequency effects in 1D models, but ray theoretical interpre-

140 tations can badly misrepresent the strength and orientation of anisotropy when lateral
 141 variations in anisotropy may exist (Nowacki & Wookey, 2016).

142 The different phases have different sensitivity to the anisotropic tensor due to their
 143 propagation angle and the length of their propagating path across the lowermost man-
 144 tle (Figure 2). S_{diff} has long horizontal propagation paths in the mantle, and therefore
 145 good sensitivity to radial anisotropy. SKS propagates at sub-vertical angles (18° – 33°)
 146 across the lowermost mantle, so splitting is caused by the component of azimuthal anisotropy,
 147 i.e. variation of wave speed in the horizontal plane. SKKS (40° – 50°) and ScS (62° – 78°)
 148 propagate at intermediate angles, and are sensitive to tilted anisotropy. While early stud-
 149 ies focused mainly on constraining the radial anisotropic component (e.g., Young & Lay,
 150 1990; Matzel et al., 1996; Garnero & Lay, 1997), recent studies interpret their observa-
 151 tions as tilted anisotropy, the main component constrained when accounting for the in-
 152 cidence angles in the lowermost mantle (e.g., Thomas et al., 2007; Wookey & Kendall,
 153 2008; Nowacki et al., 2010).

154 One additional, unique type of observation worth mentioning are polarity obser-
 155 vations of phases bouncing off of the so-called D'' discontinuities in the lowermost man-
 156 tle (Thomas et al., 2011; Cobden & Thomas, 2013; Creasy et al., 2019; Pisconti et al.,
 157 2019). Azimuthal variations in the polarity measurements suggest these are sensitive to
 158 underlying anisotropy. As observations can be applied to S and P reflections (‘SdS’, and
 159 ‘PdP’), they are to our knowledge the only body wave studies that have resolved a com-
 160 ponent of both S and P wave anisotropy for a single location.

161 Most observational studies focus on a single observational method, as well as a sin-
 162 gle azimuthal direction. To sufficiently constrain anisotropy in a single location to uniquely
 163 interpret flow direction, multiple techniques need to be combined (Creasy et al., 2019).
 164 Efforts have been made to target a single region from multiple angles using ScS (Nowacki
 165 et al., 2010; Wookey & Kendall, 2008) and polarisation measurements (Thomas et al.,
 166 2011), as well as combining multiple angles with multiple body wave phases (Ford & Long,
 167 2015; Creasy et al., 2019; Wolf et al., 2019).

168 **2.3 Observed regional anisotropy**

169 This is not an exhaustive overview of body wave studies and for a full table of stud-
 170 ies we refer to Romanowicz & Wenk (2017). Here we highlight consistencies across these

171 studies, mainly focusing on more recent studies which benefit from increased coverage
 172 by seismic arrays. Regional body wave studies largely agree with tomographic models
 173 on geographical trends in radial anisotropy, i.e. $\xi > 1$ where isotropic velocities are fast,
 174 and $\xi < 1$ where isotropic velocities are slow (e.g., Wookey & Kendall, 2007; Kawai &
 175 Geller, 2010). Models interpreting tilted anisotropy have overwhelmingly sampled isotrop-
 176 ically fast areas and many find a sub-horizontal fast axis and thus a component of $\xi >$
 177 1 (e.g., Thomas et al., 2007; Garnero et al., 2004; Wookey & Dobson, 2008; Nowacki et
 178 al., 2010), while several studies find a fast axis which is tilted from the horizontal by around
 179 45° (Wookey et al., 2005; Cottaar & Romanowicz, 2013), which is not compatible with
 180 radial anisotropy. Particularly, regions just outside of LLSVPs appear to have strong and
 181 variable anisotropy, as is observed along the boundaries of the African LLSVP (Wang
 182 & Wen, 2007; Cottaar & Romanowicz, 2013; Lynner & Long, 2014; Grund & Ritter, 2019;
 183 Romanowicz & Wenk, 2017; Reiss et al., 2019), the Pacific LLSVP (Deng et al., 2017),
 184 and the Perm Anomaly (M. D. Long & Lynner, 2015). These observations show stronger
 185 anisotropy outside of the LLSVP and little to no anisotropy within the LLSVP, both in
 186 terms of tilted anisotropy (Cottaar & Romanowicz, 2013) and in terms of azimuthal anisotropy
 187 (e.g., Lynner & Long, 2014; Grund & Ritter, 2019). A change in sign from $\xi > 1$ to $\xi <$
 188 1 is also observed towards the base of the Icelandic plume (Wolf et al., 2019).

189 While some consistency emerges on the types of anisotropy, and correlations with
 190 isotropic velocities, uncertainty lies in the strength of anisotropy observed. Tomographic
 191 models contain radial anisotropy on the order of several %, and amplitudes vary between
 192 models (see Figure 1). Local observations interpret tilted anisotropy of 0.8–1.5% across
 193 a layer of 250 km beneath North America (Nowacki et al., 2010) and up to 8% across
 194 150 km beneath the Antarctic Ocean (Cottaar & Romanowicz, 2013). Such variations
 195 could represent true geographical observations, but biases could also occur as propaga-
 196 tion angles used might not be optimal to observe the strongest splitting or assumed layer
 197 thicknesses. In these two example studies, interpreted amplitudes might also differ as
 198 one is interpreted ray-theoretically (Nowacki et al., 2010) and one by forward modelling
 199 (Cottaar & Romanowicz, 2013). Potentially, consistently constrained relative amplitudes
 200 in splitting might help map lateral variations in flow strength or direction.

210 **3 Forward modelling**

211 To provide synthetic tests for the hypothesis that anisotropy is caused by crystal
 212 preferred orientation (CPO), multi-disciplinary models are built that span many spa-
 213 tial scales (see flow chart in Figure 3). Geodynamic models provide maps of strain across
 214 10s to 1000s of km. The strain observed is accommodated on the micro scale by defor-
 215 mation mechanisms in a set of crystals, assuming a degree is accommodated by dislo-
 216 cation glide to create preferential orientation. The individual elastic constants of each
 217 of the deformed set of crystals are averaged using their orientations, giving the fully anisotropic
 218 tensor for a single location. This process needs to be repeated for many locations, to pro-
 219 vide an anisotropic model with signatures that can be observed over 10s or 100s of km
 220 by seismic waves. Here we explain the main choices and assumptions made in these mod-
 221 els.

222 While we focus on the hypothesis that CPO is the cause of seismic anisotropy in
 223 the lowermost mantle, studies have forward modelled the potential of shape preferred
 224 orientation (SPO) as well. SPO anisotropy is caused by layering or inclusions of strongly
 225 heterogeneous (but potentially intrinsically isotropic) material (Kendall & Silver, 1998;
 226 Hall et al., 2004; Creasy et al., 2019; Reiss et al., 2019). In the case of inclusions, anisotropy
 227 can be observed in the effective medium to which the waves are sensitive if a degree of
 228 alignment or preferred orientation persists over a broad area. This alignment of inclu-
 229 sions would result from local deformation, and thus also contain information about man-
 230 tle flow. However, studies observing high frequency scatterers in the lowermost mantle
 231 observe very weak velocity contrasts ($<0.1\%$: Mancinelli & Shearer, 2013). Extremely
 232 strong isotropic velocity anomalies (10–30%) are only observed in thin patches of sev-
 233 eral 10s of km on top of the core–mantle boundary, the so-called ultra-low velocity zones
 234 (e.g., Garnero et al., 1998; Yu & Garnero, 2018).

239 **3.1 Geodynamic models**

240 Assumptions on the flow occurring in the lowermost mantle have varying degrees
 241 of complexities. In the simplest of models, horizontal flow is assumed causing simple hor-
 242 izontal shear as one might expect in a iso-chemical thermal boundary layer (as used in
 243 Wookey & Kendall, 2007). Anisotropy observed, however, does not have to represent lo-
 244 cal deformation, but could represent fossilized anisotropy. Anisotropic material can be

245 formed elsewhere and be transported and rotated without overriding the preferred ori-
246 entation. Therefore it is important to track the history of deformation for material in
247 a given location. To represent change in flow direction in downwellings and upwellings
248 in the lowermost mantle, corner flow streamlines can be used (Tommasi et al., 2018).

249 A range of studies use fully numerical models, where a number of assumptions on
250 parameters for the lower mantle need to be made. The history of deformation is tracked
251 by passive tracers that are advected through the model and record the velocity gradi-
252 ent at each step. The deformation history is generally used from the top of the lower man-
253 tle (e.g., Cottaar et al., 2014), or from the bridgmanite to post-perovskite transition (e.g
254 Walker et al., 2011).

255 In one approach (Cottaar et al., 2014; Chandler et al., 2018), the CitcomS program
256 (Zhong et al., 2000) is used to solve for the conservation of mass, momentum and en-
257 ergy, in a system that is heated from below, and where a slab is forced down from the
258 top. Tracers are introduced at the top of the slab, and a large number of them eventu-
259 ally end up in the lowermost mantle, although the final distribution is irregular and shows
260 clumping of tracers.

261 In a different approach (Walker et al., 2011; Nowacki et al., 2013), the flow field
262 is the instantaneous flow predicted by isotropic wave velocities, the gravity field, a 1D
263 viscosity model, and other geophysical constraints (Simmons et al., 2009). Because the
264 inversion assumes that flow does not change with time, regularly-spaced tracers can be
265 back-propagated to the top of D'' across the flow field, after which they are forward prop-
266 agated to track the deformation along the path. The advantage of this method is that
267 one retrieves a regularly-sampled global anisotropic model that holds some potential re-
268 lationship to the isotropic velocities, and that can thus be compared to global or regional
269 seismic observations. Additionally, this method tests a prior assumed relationship be-
270 tween isotropic velocities and the flow field, testing models of thermal and/or thermo-
271 chemical heterogeneity in the lower mantle.

272 While these geodynamical models represent test cases to explain lowermost seis-
273 mic anisotropy, they are simplified in many ways. The geodynamical models have not
274 explicitly included the bridgmanite to post-perovskite transitions, which only has a small
275 density jump (Murakami et al., 2004; Oganov & Ono, 2004), but would cause significant
276 viscosity weakening (Hunt et al., 2009) and allow slab material to spread more easily (Nak-

277 agawa & Tackley, 2011). The viscosity model would be even more complex if the forma-
 278 tion of CPO could be fed back into the geodynamical model creating anisotropic viscos-
 279 ity. So far, models have not tested the hypothesis of LLSVPs representing a different com-
 280 position (e.g., Garnero et al., 2016), which appears important to understand the later-
 281 ally varying anisotropy around LLSVP boundaries.

282 3.2 Mineralogical constraints

283 In the upper mantle, the mineral olivine is abundant, and, with a highly anisotropic
 284 crystal, represents a straightforward candidate to explain CPO anisotropy (Becker and
 285 Lebedev, this volume). For the lowermost mantle the debate is still open as to which min-
 286 eral or polymineralic assemblage can explain the observed anisotropy. For a candidate
 287 mineral or assemblage, we need to know its single crystal elasticity, which depending on
 288 crystal symmetry can be described by three to 21 independent parameters. We mostly
 289 rely on first-principle or *ab initio* calculations which solve the electronic Schrödinger equa-
 290 tion to obtain the crystal structure and the elasticity at high pressures and temperatures
 291 (Buchen, this volume). Merely obtaining isotropic average elasticity information from
 292 experiments under these extreme conditions is very challenging, let alone measuring the
 293 independent anisotropic parameters (e.g., Marquardt et al., 2009; Finkelstein et al., 2018).

294 Additionally, we need to know how the candidate mineral or assemblage deforms
 295 (Miyagi, this volume). To create seismic anisotropy, a mineral must significantly deform
 296 by dislocation glide. In dislocation glide, dislocations within the crystal move along crys-
 297 tallographic planes. Preferred orientation results when crystals rotate to accommodate
 298 glide along its weakest glide planes. Other mechanisms like diffusion creep or disloca-
 299 tion climb are not usually thought to cause preferred orientation, though this is not al-
 300 ways the case (Wheeler, 2009, 2010; Dobson et al., 2019). If dislocation glide is the pre-
 301 ferred mechanism, the next question that arises is what are the relative strengths of the
 302 different slip systems (i.e., glide plane and slip directions). Calculations explore the rel-
 303 ative strengths of different deformation mechanisms and glide systems by calculating lat-
 304 tice friction and forces required to slip a dislocation (Peierls stress) in atomistic mod-
 305 els (Walker et al., 2010; Cordier et al., 2012). Experimentally, slip system activities can-
 306 not usually be measured for single crystals of the phases of interest here. Instead, ma-
 307 terials are deformed under compressive or shear stress in a large-volume apparatus (usu-
 308 ally on analogue materials), or in a diamond-anvil cell (For further details ?Romanow-

309 icz & Wenk, 2017) The resulting deformation may be imaged by X-ray diffraction. Dom-
 310 inant slip systems may be estimated by inspection of the orientation distribution func-
 311 tions (ODFs) of the crystallographic planes of interest, or inverted for by comparing for-
 312 ward calculations of the experimental deformation with the results obtained.

313 To determine macroscopic anisotropy from these mineralogical constraints, the set
 314 of slip systems are combined with a deformation tensor to model a set of deformed crys-
 315 tals. Most often this is done using a homogenisation method such as the viscoplastic self-
 316 consistent method (VPSC; Lebensohn & Tomé, 1993).

317 Forming the majority of the lowermost mantle, and thus the likeliest candidates
 318 to be the anisotropy-causing phases, are bridgmanite, post-perovskite and ferropericlase.

319 **3.2.1 Bridgmanite**

320 Bridgmanite, (Mg,Fe)SiO₃-perovskite, is the most abundant mineral in the lower
 321 mantle (and in the Earth). Its pure Mg-endmember shows ~11% P wave and up to 15%
 322 S wave anisotropy (Oganov et al., 2001; Wentzcovitch et al., 2006; Stackhouse, Brodholt,
 323 Wookey, et al., 2005), and shows little (Li et al., 2005; Zhang et al., 2016) or variable (Fu
 324 et al., 2019) variation with the inclusion of iron.

325 There are mixed results on bridgmanite being a suitable candidate to explain anisotropy.
 326 Both experiments and calculations proposed a dominant glide plane of (001) (Wenk et
 327 al., 2004; Merkel et al., 2007; Ferré et al., 2007) which results in the opposite radial anisotropy
 328 to that observed (e.g., Wenk et al., 2011), while other experiments and calculations ar-
 329 gue for a dominant (100) glide plane (Mainprice et al., 2008; Tsujino et al., 2016), which
 330 can create the observed $V_{SH} > V_{SV}$ in simple shear. Miyagi & Wenk (2016) report a
 331 change from (001)-dominated glide to (100) around 55 GPa.

332 Bridgmanite is also known to be a very strong mineral. Experiments deforming a
 333 multi-phase mixture of bridgmanite and a smaller fraction of the weaker phase ferroper-
 334 iclase (or analogs), show in some cases that the ferropericlase takes up the majority of
 335 the deformation (Girard et al., 2016; Kaercher et al., 2016; Miyagi & Wenk, 2016), while
 336 in others the strong bridgmanite phase still dominates deformation (Wang et al., 2013)
 337 in line with simulations in a finite element model (Madi et al., 2005). Recently atom-
 338 istic calculations have shown that the resistance to dislocation glide is very high, and dis-

339 location climb should dominate (Boioli et al., 2017). Dislocation climb dominance could
 340 explain the general lack of anisotropy across most of the lower mantle, as well the high
 341 viscosity of the lower mantle (Reali et al., 2019). However, attempts to explain weak anisotropy
 342 around ponded subducted slabs in the uppermost lower mantle in terms of bridgman-
 343 ite CPO (Tsujino et al., 2016; Walpole et al., 2017; Ferreira et al., 2019; Fu et al., 2019)
 344 would be therefore puzzling.

345 **3.2.2 Post-perovskite**

346 Post-perovskite is a high-pressure polymorph of bridgmanite, which could become
 347 stable in the lowermost mantle (Murakami et al., 2004; Oganov & Ono, 2004). Compared
 348 to bridgmanite, post-perovskite is (1) more anisotropic (Iitaka et al., 2004; Stackhouse,
 349 Brodholt, & Price, 2005; Wentzcovitch et al., 2006; Zhang et al., 2016), and (2) much
 350 weaker to deform (Hunt et al., 2009; Ammann et al., 2010; Goryaeva et al., 2016). There-
 351 fore it is an attractive candidate to explain anisotropy observed in the lowermost man-
 352 tle. If, and to what degree, post-perovskite is actually stable at the pressures in the low-
 353 ermost mantle is still up for debate (see overviews in Cobden et al. (2015) and Hirose
 354 et al. (2015)), but invoking the presence of post-perovskite helps explain S-to-P veloc-
 355 ity ratios in the lowermost mantle (P. Koelemeijer et al., 2018). If present, the strongly
 356 positive Clapeyron slope of its phase transition from bridgmanite implies post-perovskite
 357 is stable in a thicker layer in cold regions than in hot regions (Oganov & Ono, 2004; Tsuchiya
 358 et al., 2004). Potentially post-perovskite becomes unstable again in the thermal bound-
 359 ary layer close to the core-mantle boundary, creating a lens of post-perovskite (Hernlund
 360 et al., 2005).

361 Testing post-perovskite as a candidate to explain anisotropy is difficult as the pre-
 362 ferred slip system of post-perovskite is uncertain and diamond-anvil cell experimental
 363 results have varied widely over the past 15 years (For further details, see ?, in this vol-
 364 ume.). The most recent results can be split in two categories. Experiments using MgSiO_3
 365 post-perovskite, and MnGeO_3 or MgGeO_3 analogs, show a preferred slip plane of (001)
 366 (e.g., Miyagi et al., 2010; Hirose et al., 2010; Nisr et al., 2012; X. Wu et al., 2017). Ex-
 367 periments using CaIrO_3 postperovskite as an analog show a dominant slip system of $[100](010)$
 368 (where $[hkl]$ gives the Burgers vector; e.g., Yamazaki et al., 2006; Niwa et al., 2012; Hunt
 369 et al., 2016). Atomistic models confirm the results of the latter category, showing both
 370 slip systems $[100](010)$ and $[001](010)$ (Cordier et al., 2012; Goryaeva et al., 2015, 2017)

371 as well as the occurrence of twinning $1/2 \langle 110 \rangle \{1\bar{1}0\}$ (Carrez et al., 2017). Addi-
 372 tionally, it is suggested that post-perovskite could inherit preferred orientation or tex-
 373 ture through the phase transition from bridgmanite (Dobson et al., 2013). Interpreta-
 374 tion of the texture inheritance in deformation experiments has been specifically argued
 375 to explain part of the variation in interpreted preferred glide plane (e.g., Walte et al.,
 376 2009; Miyagi et al., 2011). This could only be the case if bridgmanite forms CPO tex-
 377 ture due to dislocation glide, which is debatable (Boioli et al., 2017). A more feasible sce-
 378 nario is bridgmanite inheriting texture from post-perovskite in a reverse transition which
 379 could occur in the hotter regions (Dobson et al., 2013; Walker et al., 2018).

380 The importance of the incorporation of aluminium and iron into post-perovskite
 381 for our purposes depends on its effect on the stability field, deformation mechanisms, rhe-
 382 ology and single-crystal anisotropy of the non-endmember phase. Iron- and aluminium-
 383 bearing post-perovskite is likely to be as anisotropic as the magnesian end-member at
 384 lowermost mantle conditions (Zhang et al., 2016), but there is little evidence for its
 385 effect on plasticity. Recent work suggests that iron will strongly partition into ferroper-
 386 iclase in the lowermost mantle in any event (?), thus its importance may be limited.

387 **3.2.3 Ferropericlase**

388 Ferropericlase (Mg, Fe)O is present in the lower mantle with a molar abundance
 389 of 10–30% (e.g., McDonough & Sun, 1995). Before post-perovskite was discovered in 2004,
 390 ferropericlase was already considered a potential explanation of lowermost mantle anisotropy
 391 (Yamazaki & Karato, 2002). It is cubic, and its elasticity can thus be described by three
 392 independent parameters. These are constrained both through *ab initio* calculations (Karki
 393 et al., 2000; Z. Wu et al., 2013) and through experiments (e.g., Jackson et al., 2006). The
 394 results of these studies show significant single crystal anisotropy, as well as an increase
 395 of anisotropy with Fe content, related to changes in C_{12} and C_{44} with cell volume via
 396 pressure (Marquardt et al., 2009; Antonangeli et al., 2011; Finkelstein et al., 2018).

397 Ferropericlase is much weaker than bridgmanite (Cordier et al., 2012). Atomistic
 398 calculations of pure MgO endmember have shown dominating slip systems of $\langle 110 \rangle \{1\bar{1}0\}$
 399 and $\langle 110 \rangle \{100\}$ (Carrez et al., 2009; Amodeo et al., 2011, 2016). Experiments on pure
 400 MgO (Merkel et al., 2002; Girard et al., 2012) and (Mg, Fe)O (Lin et al., 2009) show dom-
 401 inant slip on $\langle 110 \rangle \{1\bar{1}0\}$, while higher temperature experiments on (Mg, Fe)O also ac-

402 tivate $\langle 110 \rangle \{100\}$, consistent with the calculations. Whether ferropericlase can explain
 403 the observed anisotropy depends on the degree of single crystal anisotropy (related to
 404 the Fe content), its abundance in the lowermost mantle (i.e. whether ferropericlase grains
 405 become interconnected), and the general strength contrast between ferropericlase and
 406 bridgmanite or post-perovskite. However, it should be noted that even in the two-phase
 407 experiments discussed earlier, where ferropericlase takes up the bulk of the deformation,
 408 coherent CPO does not develop in the ferropericlase, potentially due to the polyphase
 409 geometry causing strain heterogeneity in the ferropericlase crystals (Kaercher et al., 2016;
 410 Miyagi & Wenk, 2016).

411 *3.2.4 Other phases*

412 Whilst post-perovskite, bridgmanite and ferropericlase are expected to dominate
 413 the lowermost mantle, it is possible that other phases play a role in causing anisotropy.

414 Though peridotite comprises $\sim 5\%$ of Ca-perovskite (CaMgSiO_3) in the lower man-
 415 tle, basaltic compositions may hold up to 30% (McDonough & Sun, 1995), and hence
 416 Ca-pv may be important if subducted material can accumulate at the base of the man-
 417 tle. Sample recovery issues mean that high-pressure and -temperature experiments are
 418 difficult and the phase boundary between cubic and tetragonal Ca-pv is still being de-
 419 termined (Thomson et al., 2019), but molecular dynamics simulations (Li et al., 2006)
 420 show maximum single-crystal shear wave anisotropy of 25%, similar to other phases men-
 421 tioned here. Room-temperature diamond-anvil cell experiments (Miyagi et al., 2009) and
 422 Peierls–Nabarro modelling (Ferre et al., 2009) suggest Ca-pv might form a CPO in de-
 423 formation by glide on the cubic slip system $\langle \bar{1}\bar{1}0 \rangle \{110\}$, and experiments on the analogue
 424 CaGeO_3 suggest Ca-perovskite may be weaker than MgO (Wang et al., 2013), but rel-
 425 atively few studies have yet examined this further.

426 Silica phases may also make up $\sim 20\%$ of a basaltic lower mantle. While it seems
 427 likely that stishovite is stable until about 1500 km depth, uncertainty remains as to when
 428 in the lower mantle silica transitions from the CaCl_2 structure to seifertite (e.g., Sun et
 429 al., 2019). This may be important since whilst seifertite appears to be only moderately
 430 anisotropic (?) and hence is likely not be a large contributor to lowermost mantle anisotropy,
 431 CaCl_2 -type silica may have much stronger shear wave anisotropy of about 30% (?). Un-

432 fortunately we do not currently have constraints on how silica phases may accommodate
433 strain.

434 If hydrogen can be carried to the deep mantle, then hydrous phases such as alu-
435 minous phase D or phase H might occur in D'' (e.g., ??), whilst aluminous phase δ -AlOOH
436 is likely present in basaltic compositions (e.g., ?), and iron-rich regions could contain Fe-
437 rich phases such as FeO_2 or FeOOH (e.g., ?). Some of these phases may be strongly anisotropic,
438 however compared to the nominally anhydrous silicates like bridgmanite and post-perovskite,
439 little work has been done to understand their deformation mechanisms.

440 **4 Joint geodynamic–seismic modelling**

441 **4.1 Recent developments**

442 Several endeavours—mainly over the last decade—have tried to tie together all the
443 fields and constraints discussed so far, in order to interpret anisotropy in the lowermost
444 mantle. The long-term, sometimes enigmatic, goal of these studies is to map flow direc-
445 tions in the lowermost mantle to understand its role in the overall mantle convection (as
446 the title of this chapter suggests). Most studies to this date, however, attempt to con-
447 strain the underlying cause of anisotropy taking their best guess at the flow regime.

448 In terms of the cause of anisotropy, recent studies rely heavily on post-perovskite
449 being stable in the lowermost mantle to explain the observed anisotropy, arguing that
450 bridgmanite produces the wrong radial anisotropic signature, and ferropericlase is not
451 abundant enough to dominate anisotropic signatures. Bridgmanite not playing a major
452 role can also be argued in light of the recent results that bridgmanite is too strong to
453 cause dislocation glide and develop preferred orientation (Boioli et al., 2017).

454 The dominant glide plane in post-perovskite that is argued to explain anisotropy
455 varies with studies arguing for dominant glide on (010) (Walker et al., 2011; Nowacki et
456 al., 2013; Creasy et al., 2017; Tommasi et al., 2018; Ford et al., 2015) and (001) (Nowacki
457 et al., 2010; Cottaar et al., 2014; Walker et al., 2018; X. Wu et al., 2017; Chandler et al.,
458 2018). These studies range from finding a best fitting model from a qualitative compar-
459 ison to previously published observations (i.e., Cottaar et al., 2014; Tommasi et al., 2018)
460 to a quantitative misfit with local observations (Nowacki et al., 2010; Ford et al., 2015;
461 Creasy et al., 2017) or with global anisotropic models (Walker et al., 2011, 2018). Of course,
462 all of these studies have made different assumptions and choices, which may affect the

463 final conclusion. One example is the choice of elastic constants—for instance, a domi-
 464 nant glide system on the (010) plane results in $V_{SH} > V_{SV}$ when using elastic constants
 465 of Stackhouse, Brodholt, & Price (2005), and in $V_{SV} > V_{SH}$ when using those of Wentz-
 466 covitch et al. (2006) (Yamazaki & Karato, 2007; Wenk et al., 2011). Similarly, studies
 467 may choose to use constants derived at a single pressure and temperature—not neces-
 468 sarily those of the part of the mantle of interest—or attempt to include the variable anisotropic
 469 effects as P and T vary (Walker et al., 2011).

470 A number of recent studies are worth highlighting. Tommasi et al. (2018) explore
 471 the anisotropy resulting from deformation constraints from atomistic modelling instead
 472 of experimental results, arguing for a dominant glide plane of (010). Atomistic calcula-
 473 tions, which will hopefully converge with experimental results in the future, offer a great
 474 step forward into constraining the deformation in the lowermost mantle. Their modelling
 475 finds weak radial anisotropy of $V_{SH} > V_{SV}$ and sub-horizontal fast polarization direc-
 476 tions in simple corner flow.

477 Their modelled elastic tensors with post-perovskite and periclase in an upwelling
 478 tracer can also fit the recent observations of changing anisotropy beneath Iceland by Wolf
 479 et al. (2019). However, the paper also presents models of pure bridgmanite and periclase
 480 that can fit the observations for the assumed change in flow.

481 Walker et al. (2018) explore texture inheritance from (001) slip in post-perovskite
 482 to bridgmanite (Dobson et al., 2013) on a global scale. Such a model can explain the ob-
 483 served sharp changes in the signature of anisotropy from regions dominated by cold down-
 484 wellings, to regions dominated by hot upwellings or LLSVPs. Comparable results for tex-
 485 ture inheritance were shown by Chandler et al. (2018) using the tracking of single trac-
 486 ers from downwelling to upwelling.

487 Most of the studies mentioned have pre-assumed the flow pattern either locally or
 488 globally and the models of different compositions are tested against seismic observations.
 489 Only the studies of Ford et al. (2015) and Creasy et al. (2017) both fit the compositional
 490 model as well as the flow direction. For both cases, this is applied to one locality where
 491 anisotropy is constrained from different azimuthal directions. Ford et al. (2015) suggest
 492 mainly vertical flows occur just to the East of the African LLSVP, while Creasy et al.
 493 (2017) suggest horizontal flows in a region of fast isotropic velocities beneath New Zealand
 494 and Australia.

4.2 Example case: comparing a model to seismic observations

Many of the multi-disciplinary modelling studies discussed above compare their synthetic elasticity models to ray-theoretically derived local body wave observations. A number of studies explore the limitations of interpreting body waves observations in terms of anisotropy by analysing synthetic observations; for example for 1D isotropic or radially anisotropic models for S_{diff} waves (Maupin, 1994; Komatitsch et al., 2010; Borgeaud et al., 2016; Parisi et al., 2018) and for ScS waves (Kawai & Geller, 2010). Nowacki & Wookey (2016) extend the analysis for ScS waves to full synthetic anisotropic models with small-scale variations from the model of Walker et al. (2011) (cf. Figure 3). They conclude that ray-theoretical interpretations hold up for the simplest anisotropic models, but break down for those with variable anisotropy. Additionally, the finite-frequency wave senses less splitting than a ray-theoretical interpretation of an anisotropic model would suggest, as the finite-frequency sensitivity will average over the strongly varying anisotropic medium, sensing an effective medium.

Here we explore these limitations further by combining the forward modelling in a subducting slab of Cottaar et al. (2014) with the full-wave modelling of Nowacki & Wookey (2016) and analyse S_{diff} , ScS, SKS, and SKKS phases in a finite-frequency framework.

4.2.1 Geodynamic and texture modelling

We use the results of Cottaar et al. (2014). We refer the reader to the original work for a full description of parameters used, but note that in this type of modelling, uncertainty can be introduced via a number of parameters including: the chosen relative critical resolved shear stresses on each slip system; the lack of a non-glide mechanism to accommodate strain and reset texture (such as diffusion creep); the phase boundary between phases; the single-crystal elastic constants; and the stress-strain homogenisation scheme. In the following we give a short summary of the modelling details.

Deformation is tracked along tracer particles (Figure 4a) across the lowermost mantle using CitcomS (Zhong et al., 2000), where 500 grains are modelled with the viscoplastic self-consistent method (VPSC; Lebensohn & Tomé, 1993) to accommodate the deformation. 75% of these grains are post-perovskite ('ppv') or bridgmanite ('pv'), and 25% are periclase. For post-perovskite, a dominant glide plane of (100) ('ppv 100' model), (010) ('ppv 010'), or (001) ('ppv 001') is assumed. The assumed glide planes for periclase are

543 **Table 1.** Summary of synthetic paths used to investigate anisotropy in the geodynamic slab
 544 model.

Code	Description, phases ^a	Source longitude (°)	Source latitude (°)	Focal mechanism ^b
A	Across slab: SKS–SKKS	0	–90	090/0/–90
B	Along slab: SKS–SKKS, S _{diff}	–55	0	180/30/0
C	Along slab: ScS, S _{diff}	0	0	280/30/–90

^a Phases analysed from full-wavefield synthetics.

^b Given as strike/dip/rake of the fault plane in °.

All events at 650 km depth.

526 weaker, and this phase ends up accommodating 35-40% of the deformation. For the elas-
 527 tic constants, the values of Stackhouse, Brodholt, Wookey, et al. (2005) are used for post-
 528 perovskite and bridgmanite, and those of Karki et al. (2000) for periclase. Cottaar et
 529 al. (2014) note that model ppv 001 is in general agreement with the radial anisotropy
 530 observed at the bottom of slabs and fast directions of azimuthal anisotropy is parallel
 531 to flow directions. The radial anisotropy in model ppv 010 also has the right sign, but
 532 is very weak in nature.

533 *4.2.2 Seismic modelling*

534 We seek to compare the predicted seismic characteristics of our geodynamic slab
 535 model to regional observations of anisotropy, including splitting in S_{diff}, SKS–SKKS and
 536 S–ScS differential splitting, as well as observations of changes in splitting intensity (Chevrot,
 537 2000). In order to do this, we simulate the propagation of waves through the model in
 538 two directions—along the slab and across it—for a range of geometries. We use synthet-
 539 ics in the epicentral distance range $55^\circ \leq \Delta \leq 80^\circ$ for ScS, $100^\circ \leq \Delta \leq 130^\circ$ for
 540 SKS, $110^\circ \leq \Delta \leq 130^\circ$ for SKKS and $95^\circ \leq \Delta \leq 120^\circ$ for S_{diff}. Table 1 outlines the
 541 geometries used in this study and which phases are investigated for each, whilst Figure 4b
 542 shows the location of the events and receivers.

560 We calculate the seismic response of the slab using the spectral element method
 561 as implemented in the SPEC-FEM3D-GLOBE code (Komatitsch & Tromp, 2002). In or-

562 der to remove time in writing intermediate files, we use a version of the code where cre-
 563 ating the spectral element mesh and solving the equations of motion are performed in
 564 the same program (Komatitsch et al., 2003; Nowacki & Wookey, 2016). We use two chunks
 565 of the cubed sphere with 800 spectral elements along each side, giving seismograms ac-
 566 curate at frequencies below 0.2 Hz, similar to the dominant period of the waves at these
 567 distances.

568 The elasticity model is mapped to the seismic computational mesh by finding the
 569 nearest neighbouring tracer particle within a defined ‘slab’ region, which is below 400 km
 570 above the CMB and within 150 km from any given particle. Beyond this distance, the
 571 nearest particle’s elasticity grades smoothly to the background 1D velocity, given by AK135
 572 (Kennett et al., 1995), over a 100 km distance using Voigt averaging between the isotropic
 573 and full elastic tensor. This smoothing distance was chosen to avoid artificially extend-
 574 ing the region of the mantle influenced by the slab, whilst avoiding seismic artifacts from
 575 a spatially abrupt transition between isotropic and anisotropic mantle.

576 *4.2.3 Synthetic analysis*

577 We can process synthetics from our forward model in the same way as data and
 578 compare the two. For the purposes of this example, we show a selection of results for the
 579 three paths, for different combinations of seismic phases, analysing the shear wave split-
 580 ting in ScS, S_{diff}, and differential splitting between SKS and SKKS. In all cases, we anal-
 581 yse the shear wave splitting in a window around the arrival of interest using the minimum-
 582 eigenvalue method of Silver & Chan (1991), with errors as updated by Walsh et al. (2013).
 583 The fast axis here is defined as the angle ϕ' from the radial component (or the vertical
 584 at the bottoming point of the seismic ray, Figure 1c in Nowacki et al. (2010)). We also
 585 consider the splitting intensity (SI; Chevrot, 2000) for SKS and SKKS waves, where the
 586 polarisation is known to be radial, and S_{diff} waves, where almost all SV energy is lost
 587 along the diffracted path, rendering them horizontally polarised. For this reason, S_{diff}
 588 SI is calculated in the opposite sense to usual for SK(K)S waves, interchanging the ra-
 589 dial and transverse components in the calculation. Discrepant SKS–SKKS splitting pairs
 590 are identified where either one of the phases shows null splitting, whilst the other does
 591 within error, or the two phases’ 95% confidence region of the small-eigenvalue surface
 592 do not overlap. Additionally, for all splitting measurements we use the automatic clas-

sification method of Wuestefeld et al. (2010) to calculate Q , a measure of quality between
 –1 and 1. –1 indicates a null, 1 a good measurement, and 0 a likely poor measurement.

We consider first the splitting in ScS for path ‘C’ (Figure 5). This path is similar
 to observations of splitting along palaeosubduction zones such as beneath the Caribbean
 (Garnero et al., 2004; Maupin et al., 2005; Nowacki et al., 2010, e.g.,). In general, it seems
 that $\phi' \approx 90^\circ$ ($\xi > 1$) in many slab regions (Nowacki et al., 2011; Romanowicz & Wenk,
 2017); in the Caribbean in particular, Garnero et al. (2004) infer a systematic rotation
 in the fast angle across the palaeoslab region, giving a change in ϕ' from $\sim 105^\circ$ to \sim
 75° .

Returning to Figure 5, it is clear that plasticity models ppv 010 and ppv 100 are
 better candidates than the remaining models at reproducing the $V_{SH} > V_{SV}$ and vari-
 able ϕ' signals seen in data. Note that this is a different conclusion from Cottaar et al.
 (2014), which could be due to the added complexity in this study of investigating the
 non-horizontal orientation of the waves, which can cause rotations in ϕ' (see Figure 2).
 The models produce values of δt which are mostly comparable to those seen in nature,
 though larger at up to 6 s in the synthetics versus ~ 2 –3 s as observed. The strength of
 anisotropy present in the models is up to $A^U = 0.1$, which is about one-third of the pre-
 dicted single crystal anisotropy of ppv in the lowermost mantle (Stackhouse, Brodholt,
 Wookey, et al., 2005).

We next show results for path ‘B’, which samples the slab similarly, but using S_{diff}
 and SKS–SKKS phases, in Figures 6 and 7. SI for S_{diff} should be large only when a sig-
 nificant non-radial anisotropy is present, which is generally the case within and at the
 edges of the slab.

It is notable in all cases that the pattern of ϕ' and δt is complex and variable across
 the slab, with large regions of null splitting even where strong anisotropy is present. Null
 splitting may occur when the polarisation of a shear wave travelling through an anisotropic
 medium is close to the fast or slow shear wave orientations (which are perpendicular)
 in that direction, and this may be the cause here. Variability in ϕ' is expected because
 of the pattern of flow in the model, and we observe fairly smooth rotations of ϕ' from
 north to south in the ppv models, similarly to data. However, the pv case shows δt vari-
 ations do not correlate strongly to simple features in the elasticity model. This illustrates
 the sometime non-intuitive manner in which the seismic wave averages structure, and

646 cautions against the use of approximate methods like ray theory when calculating syn-
 647 thetics in such models for data comparison.

648 SKS–SKKS pairs, in contrast, show relatively straightforward behaviour, with dis-
 649 crepant pairs concentrating near the edges of the high-anisotropy areas as expected. The
 650 ‘core’ of the deformed material does not show discrepant splitting, as both phases show
 651 similar behaviour. Notably, for ppv 001 there is a region in the northeast which does not
 652 show the expected behaviour. We see a similar non-intuitive behaviour in path A (Fig-
 653 ure 4b). Here, although some discrepant pairs straddle the edge of the slab for ppv 001,
 654 very few paths show this for any of the other models. Inferring the edges of anisotropic
 655 regions therefore must again be done with caution.

656 We also examine the raw difference in splitting intensity between SKS and SKKS
 657 at the same seismograms, $\Delta SI = SI_{SKS} - SI_{SKKS}$ (Figure 8). Measuring ΔSI is com-
 658 putationally simple, and hence holds the promise for automatic global mapping of D''
 659 anisotropy. Comparing with the differential splitting predictions (Figures 4c, 6 and 7),
 660 it appears that the along-slab path B (Figure 8b) shows straightforward behaviour, where
 661 ΔSI deviates significantly from 0 where the slab is significantly anisotropic, either pos-
 662 itively or negatively depending on the exact elastic structure in the model. This agrees
 663 well with the differential splitting interpretation. For path A, however (Figure 8a), a large
 664 negative ΔSI signal is present at the eastern end of most models, though this is not cor-
 665 related to significant differential splitting (Figure 4c). Most models also show large ΔSI
 666 in the central northern part, but again this is not reflected in differential splitting. This
 667 suggests that although there is significant difference between the elastic structure expe-
 668 rienced by the SKS and SKKS waves in these regions as they cross the edge of the anisotropic
 669 part of the slab, the shear wave splitting is not sufficiently coherent and clear to provide
 670 a strong signal. Nevertheless, these calculations suggest that a more global SKS–SKKS
 671 comparison holds promise for detecting regions where anisotropy changes rapidly.

676 **5 Limitations, advances, and the way forward**

677 **5.1 The inverse problem**

678 The final goal of observing anisotropy in the lowermost mantle is, as the title of
 679 this chapter suggests, to map flow directions. We have discussed the forward model and
 680 the large number of assumptions required to create an anisotropic model and compare

681 it to seismic observations. For most studies discussed in Section 4.1 the flow model was
 682 one of the prior assumptions and different potential compositions are explored; only the
 683 recent studies of Ford et al. (2015) and Creasy et al. (2017) locally interpret flow direc-
 684 tion.

685 Results for a suite of candidate deformation mechanisms, like those in Figure 5, im-
 686 mediately make tempting a potentially circular line of reasoning: given an assumed flow
 687 model and the data, can we infer the deformation mechanism responsible for anisotropy?
 688 And with that improved estimate of deformation mechanism, can we then infer the flow
 689 field? As discussed, uncertainty as to the very cause of anisotropy in the lowermost man-
 690 tle makes such reasoning perilous. It is also worth noting that if the rheology in geody-
 691 namic models is set in part based on observations of seismic anisotropy, and the assump-
 692 tion made of a particular deformation mechanism, then there is an added danger in the
 693 use of such dynamic models to then infer the mechanism of anisotropy.

694 Despite these problems, we can proceed with caution if we hold in mind that it is
 695 the *combination* of the flow model, deformation mechanism and mineral elasticity which
 696 is being tested against the data in each instance, not any one of these in isolation. In-
 697 tuitively, varying any one of these might lead to an equally well-fitting set of synthetic
 698 observations when varying another.

699 Is finding the dominant mineral (or multi-phase system) and deformation systems
 700 creating lowermost mantle anisotropy the biggest hurdle in the way to mapping flow?
 701 If we constrain the main source of anisotropy, could we create a map of flow across the
 702 mantle? To do that, we would be interested in making a number of inverse steps (shown
 703 in Figure 3 by the white dashed arrows), each of which is non-linear and under-determined:

- 704 1. *Using the seismic observations to find the constrained parts of the seismic anisotropic*
 705 *tensor.* Constraints on the anisotropic tensor will always be limited by the prop-
 706 agation direction of the seismic phases used (Figure 2) and the azimuthal cover-
 707 age, generally leaving large parts of the anisotropic tensor unconstrained, and re-
 708 verting studies to assume symmetries (i.e. radial or azimuthal anisotropy). Ad-
 709 ditionally, the resulting anisotropic tensor would always reflect the effective elas-
 710 tic tensor that the seismic waves observed at long wavelengths, and could result
 711 from an entire suite of small-scaled heterogeneously (an)isotropic media (e.g., Backus,
 712 1962; Capdeville & Cance, 2014; Fichtner et al., 2013). In this chapter we have

frequently made the major assumption that the anisotropy of the effective tensor is due to underlying intrinsic anisotropy (CPO), and not caused by small-scale isotropic heterogeneity (SPO).

2. *Mapping from the effective anisotropic tensor to a set of textured minerals or a specific mineral with preferred orientation.* Accounting for the null-space in the elastic tensor, there would be no unique fit here and many assumptions on the mineral physics need to be made. One could not account for the entire suite of potential deformation mechanisms occurring, presence of other minerals and the related multi-phase deformation effects. With the assumption of a single dominant mineral and glide mechanism, the main imaged fast polarisation direction in the elastic tensor would be preferentially fit. There is no value in mapping the strength of the anisotropy into a degree of preferentially aligned minerals, as the amplitudes of the effective elastic tensor will be underestimated (as shown by the synthetic results in Section 4.2).

3. *Mapping from textured minerals to potential deformation history and flow directions.* A single textured mineral can result from various deformation histories as it can both reflect the deformation it is undergoing, or fossilised deformation, which could be displaced and rotated. To uniquely constrain the flow model, many observations in different locations will have to be combined, as well as including other constraints, i.e. isotropic velocities, the gravity field, and past plate tectonic models.

While we choose to highlight the true inverse steps of this problem, this poses multiple layers of non-uniqueness, which makes a flow map for the lowermost mantle based on anisotropy appear unobtainable. For the foreseeable future, mapping mantle flow will have to rely on simplified relationships between fast polarisation directions and flow with understanding of the conditions under which these are valid. For the upper mantle, a simple relationship is posed as the fast axis of deformed olivine generally aligns with the flow direction, which has allowed interpretation of asthenospheric flow from anisotropy, although the validity of under volatile-rich conditions, e.g. in the mantle wedge above subduction zones, where observations also become more complex (see Becker and Lebedev, this volume). For the lowermost mantle, Cottaar et al. (2014) pose a similar relationship between horizontal fast direction and horizontal flow direction specifically for post-perovskite with dominant (001)-glide for a simple case of a slab spreading out on

746 the CMB. Such a relationship should be tested statistically under many flow conditions,
747 rotations, and deformations, and using full-waveform modelling. Tommasi et al. (2018)
748 present a relationship of sub-parallel fast polarisation directions to the flow direction for
749 post-perovskite with dominant (010)-glide and twinning for simple horizontal flow. Their
750 study tests, not statistically but very systematically, the limitations of this relationship
751 in corner flows and the ability of different seismic phases to detect these polarisation di-
752 rections.

753 Creasy et al. (2019) pose a different question: with our current level of non-uniqueness
754 in the interpretation, how many independent seismic observations do we need in a sin-
755 gular location to interpret composition and flow? They show statistically that roughly 10
756 or more measurements of fast direction or reflection polarisations with various azimuths
757 and incidence angles are needed to uniquely constrain the anisotropic tensor to make an
758 interpretation with some confidence. It is challenging to find locations to which this can
759 be applied due to available earthquake–station geometries.

760 Whilst it is unlikely that the mineralogical parameters we have discussed will be
761 tightly constrained for some time, and similarly seismic data coverage will probably not
762 improve vastly, it is conceivable that probabilistic approaches to inferring flow from anisotropy
763 may enable progress by incorporating uncertainties in all the input parameters as in Fig-
764 ure 3 and retrieving an ensemble of acceptable flow histories. Such a model suite would
765 however likely be a vast undertaking, requiring many millions of forward iterations, in-
766 cluding geodynamic and full waveform modelling. This is unfeasible with the current com-
767 bination of forward numerical methods and computational resources, but the future may
768 bring this within our grasp.

769 5.2 Outlook

770 While mapping flow clearly remains an ambitious goal, current studies of anisotropy
771 do provide new insights into the deepest mantle. Specifically, the goal to find the source
772 of anisotropy reveals the potential importance of post-perovskite to be stable in the man-
773 tle, as bridgmanite might be too strong to cause texturing (Boioli et al., 2017) and fer-
774 ropericlase, as the minor phase, might not deform coherently (Miyagi & Wenk, 2016).
775 Observations of lateral changes in anisotropy could highlight where post-perovskite is
776 present, which relates to the temperature field and thus the convective patterns. A ma-

777 jor step forward in understanding the role of post-perovskite would be to resolve its dom-
778 inant deformation mechanisms. It remains to be seen if the latest theoretical calculations
779 (e.g., Goryaeva et al., 2017) will converge with future experimental results.

780 Studies of anisotropy are also illuminating the nature of the LLSVP boundaries.
781 From a seismological point of view, the claim that the radial anisotropy switches sign
782 inside and outside the LLSVPs needs to be further tested for its robustness. Any rela-
783 tionship between the isotropic and anisotropic velocities in tomographic models could
784 be an artefact (e.g., Chang et al., 2015). Local observations of splitting, however, have
785 confirmed strong changes in anisotropy around the edges of the LLSVPs (e.g., Cottaar
786 & Romanowicz, 2013; Wang & Wen, 2007; Lynner & Long, 2014). The nature of the LLSVPs
787 poses major unanswered questions, and understanding the changing signatures of anisotropy
788 can help resolve to what degree their boundaries represent a purely thermal or a thermo-
789 chemical gradient. In the thermal case, change in anisotropy could be explained by a phase
790 transition from post-perovskite to perovskite (Dobson et al., 2013) or by a change in flow
791 direction, likely from horizontal outside to vertical within the LLSVPs or plumes (e.g.
792 Wolf et al., 2019). In the case where LLSVPs represent thermo-chemical piles, the bound-
793 ary could also be mechanical with separate convection inside and outside the piles (e.g.,
794 Garnero & McNamara, 2008). Currently, capturing all the variation in parameters which
795 contribute to the development of anisotropy whilst correctly relating these to observa-
796 tions is computationally constrained. However, while we are far from producing a global
797 flow map based on anisotropic variations, anisotropic studies play a role in answering
798 these fundamental questions on the nature of the lowermost mantle. With the answers
799 to these questions, flow can be more easily interpreted on the basis of mapped isotropic
800 velocity variations.

801 **Acknowledgments**

802 The authors thank Andrew Walker for discussion and improvement of the manuscript,
803 and acknowledge two anonymous reviewers and editor Hauke Marquardt for helpful and
804 constructive comments. AN is supported by the Natural Environment Research Coun-
805 cil (NERC grant reference number NE/R001154/1). SC is supported by the European
806 Research Council (ERC) under the European Union’s Horizon 2020 research and inno-
807 vation programme (grant agreement No. 804071 - ZoomDeep) and the Natural Environ-

808 ment Research Council (NERC grant reference number NE/R010862/1). Computations
809 were performed on ARCHER.

810 References

- 811 Ammann, M. W., Brodholt, J. P., Wookey, J., & Dobson, D. P. (2010). First-
812 principles constraints on diffusion in lower-mantle minerals and a weak D'' layer.
813 *Nature*, *465*(7297), 462-465. doi: 10.1038/nature09052
- 814 Amodeo, J., Carrez, P., Devincere, B., & Cordier, P. (2011). Multiscale modelling of
815 MgO plasticity. *Acta Materialia*, *59*(6), 2291–2301.
- 816 Amodeo, J., Dancette, S., & Delannay, L. (2016). Atomistically-informed crystal
817 plasticity in MgO polycrystals under pressure. *International Journal of Plasticity*,
818 *82*, 177–191.
- 819 Antonangeli, D., Siebert, J., Aracne, C. M., Farber, D. L., Bosak, A., Hoesch, M.,
820 ... Badro, J. (2011). Spin crossover in ferropericlase at high pressure: A seismo-
821 logically transparent transition? *Science*, *331*(6013), 64–67.
- 822 Auer, L., Boschi, L., Becker, T. W., Nissen-Meyer, T., & Giardini, D. (2014). Sa-
823 vani: A variable resolution whole-mantle model of anisotropic shear velocity vari-
824 ations based on multiple data sets. *Journal Of Geophysical Research-Solid Earth*,
825 *119*(4), 3006-3034. doi: 10.1002/2013JB010773
- 826 Backus, G. (1962). Long-wave elastic anisotropy produced by horizontal lay-
827 ering. *Journal Of Geophysical Research*, *67*(11), 4427-4440. doi: 10.1029/
828 JZ067i011p04427
- 829 Beghein, C., Trampert, J., & van Heijst, H. J. (2006). Radial anisotropy in seis-
830 mic reference models of the mantle. *Journal Of Geophysical Research-Solid Earth*,
831 *111*(B2), B02303. doi: 10.1029/2005JB003728
- 832 Boioli, F., Carrez, P., Cordier, P., Devincere, B., Gouriet, K., Hirel, P., ... Ritter-
833 bex, S. (2017). Pure climb creep mechanism drives flow in Earth's lower mantle.
834 *Science advances*, *3*(3), e1601958.
- 835 Borgeaud, A. F., Konishi, K., Kawai, K., & Geller, R. J. (2016). Finite frequency
836 effects on apparent S-wave splitting in the D'' layer: Comparison between ray the-
837 ory and full-wave synthetics. *Geophysical Journal International*, *207*(1), 12–28.
- 838 Boschi, L., & Dziewoński, A. (2000). Whole Earth tomography from delay times
839 of P, PcP, and PKP phases: Lateral heterogeneities in the outer core or radial

- 840 anisotropy in the mantle? *Journal Of Geophysical Research-Solid Earth*, *105*(B6),
841 13675-13696.
- 842 Capdeville, Y., & Cance, P. (2014). Residual homogenization for elastic wave propa-
843 gation in complex media. *Geophysical Journal International*, *200*(2), 986–999.
- 844 Carrez, P., Ferr e, D., & Cordier, P. (2009). Peierls-Nabarro modelling of dislo-
845 cations in MgO from ambient pressure to 100 GPa. *Modelling And Simulation In*
846 *Materials Science And Engineering*, *17*(3), 035010. doi: 10.1088/0965-0393/17/3/
847 035010
- 848 Carrez, P., Goryaeva, A. M., & Cordier, P. (2017). Prediction of mechanical twin-
849 ning in magnesium silicate post-perovskite. *Scientific reports*, *7*(1), 17640.
- 850 Chandler, B., Yuan, K., Li, M., Cottaar, S., Romanowicz, B., Tomé, C., & Wenk, H.
851 (2018). A refined approach to model anisotropy in the lowermost mantle. In *Iop*
852 *conference series: Materials science and engineering* (Vol. 375, p. 012002).
- 853 Chang, S.-J., Ferreira, A. M. G., Ritsema, J., van Heijst, H. J., & Woodhouse, J. H.
854 (2015). Joint inversion for global isotropic and radially anisotropic mantle struc-
855 ture including crustal thickness perturbations. *Journal of Geophysical Research:*
856 *Solid Earth*, *120*(6), 4278-4300. doi: 10.1002/2014JB011824
- 857 Chevrot, S. (2000). Multichannel analysis of shear wave splitting. *Journal Of Geo-*
858 *physical Research-Solid Earth*, *105*(B9), 21579-21590.
- 859 Cobden, L., & Thomas, C. (2013). The origin of D'' reflections: A systematic study
860 of seismic array data sets. *Geophysical Journal International*, *194*(2), 1091–1118.
- 861 Cobden, L., Thomas, C., & Trampert, J. (2015). Seismic detection of post-
862 perovskite inside the Earth. In *The earth's heterogeneous mantle* (pp. 391–440).
863 Springer.
- 864 Cordier, P., Amodeo, J., & Carrez, P. (2012). Modelling the rheology of MgO un-
865 der Earth's mantle pressure, temperature and strain rates. *Nature*, *481*(7380),
866 177-180. doi: 10.1038/nature10687
- 867 Cottaar, S., & Lekić, V. (2016, nov). Morphology of seismically slow lower-mantle
868 structures. *Geophys. J. Int.*, *207*(2), 1122–1136. doi: 10.1093/gji/ggw324
- 869 Cottaar, S., Li, M., McNamara, A. K., Romanowicz, B., & Wenk, H.-R. (2014, Au-
870 gust). Synthetic seismic anisotropy models within a slab impinging on the core-
871 mantle boundary. *Geophysical Journal International*, *199*(1), 164-177. doi: 10
872 .1093/gji/ggu244

- 873 Cottaar, S., & Romanowicz, B. (2013). Observations of changing anisotropy across
 874 the southern margin of the African LLSVP. *Geophysical Journal International*,
 875 *195*(2), 1184-1195. doi: 10.1093/gji/ggt285
- 876 Creasy, N., Long, M. D., & Ford, H. A. (2017). Deformation in the low-
 877 ermost mantle beneath Australia from observations and models of seismic
 878 anisotropy. *Journal of Geophysical Research: Solid Earth*, *122*(7), 5243-5267.
 879 doi: 10.1002/2016JB013901
- 880 Creasy, N., Pisconti, A., Long, M. D., Thomas, C., & Wookey, J. (2019). Constraining
 881 lowermost mantle anisotropy with body waves: a synthetic modelling study.
 882 *Geophysical Journal International*, *217*(2), 766–783.
- 883 de Wit, R., & Trampert, J. (2015, November). Robust constraints on average radial
 884 lower mantle anisotropy and consequences for composition and texture. *Earth and
 885 Planetary Science Letters*, *429*, 101-109. doi: 10.1016/j.epsl.2015.07.057
- 886 Deng, J., Long, M. D., Creasy, N., Wagner, L., Beck, S., Zandt, G., . . . Minaya, E.
 887 (2017). Lowermost mantle anisotropy near the eastern edge of the Pacific LLSVP:
 888 constraints from SKS-SKKS splitting intensity measurements. *Geophysical Journal
 889 International*, *210*(2), 774–786.
- 890 Dobson, D. P., Lindsay-Scott, A., Hunt, S., Bailey, E., Wood, I., Brodholt, J. P., . . .
 891 Wheeler, J. (2019). Anisotropic diffusion creep in postperovskite provides a new
 892 model for deformation at the core–mantle boundary. *Proceedings of the National
 893 Academic of Sciences*, *116*(52), 26389-26393.
- 894 Dobson, D. P., Miyajima, N., Nestola, F., Alvaro, M., Casati, N., Liebske, C.,
 895 . . . Walker, A. M. (2013). Strong inheritance of texture between perovskite
 896 and post-perovskite in the D'' layer. *Nature Geoscience*, *6*(7), 575-578. doi:
 897 10.1038/ngeo1844
- 898 Ferré, D., Carrez, P., & Cordier, P. (2007). First principles determination of dislo-
 899 cations properties of MgSiO₃ perovskite at 30 GPa based on the Peierls–Nabarro
 900 model. *Physics of the Earth and Planetary Interiors*, *163*(1-4), 283–291.
- 901 Ferre, D., Cordier, P., & Carrez, P. (2009, January). Dislocation modeling in cal-
 902 cium silicate perovskite based on the Peierls-Nabarro model. *American Mineralo-
 903 gist*, *94*(1), 135–142. doi: 10.2138/am.2009.3003
- 904 Ferreira, A. M. G., Faccenda, M., Sturgeon, W., Chang, S.-J., & Schardong, L.
 905 (2019, April). Ubiquitous lower-mantle anisotropy beneath subduction zones.

- 906 *Nature Geoscience*, 12(4), 301. doi: 10.1038/s41561-019-0325-7
- 907 Ferreira, A. M. G., Woodhouse, J. H., Visser, K., & Trampert, J. (2010). On the ro-
 908 bustness of global radially anisotropic surface wave tomography. *Journal Of Geo-
 909 physical Research-Solid Earth*, 115, B04313. doi: 10.1029/2009JB006716
- 910 Fichtner, A., Kennett, B. L., & Trampert, J. (2013). Separating intrinsic and appar-
 911 ent anisotropy. *Physics of the Earth and Planetary Interiors*, 219, 11–20.
- 912 Finkelstein, G. J., Jackson, J. M., Said, A., Alatas, A., Leu, B. M., Sturhahn, W.,
 913 & Toellner, T. S. (2018). Strongly anisotropic magnesiowüstite in Earth’s lower
 914 mantle. *Journal of Geophysical Research: Solid Earth*, 123(6), 4740–4750.
- 915 Ford, H. A., & Long, M. D. (2015, August). A regional test of global models for
 916 flow, rheology, and seismic anisotropy at the base of the mantle. *Physics of the
 917 Earth and Planetary Interiors*, 245, 71–75. doi: 10.1016/j.pepi.2015.05.004
- 918 Ford, H. A., Long, M. D., He, X., & Lynner, C. (2015, June). Lowermost mantle
 919 flow at the eastern edge of the African Large Low Shear Velocity Province. *Earth
 920 and Planetary Science Letters*, 420, 12–22. doi: 10.1016/j.epsl.2015.03.029
- 921 French, S. W., & Romanowicz, B. (2015, September). Broad plumes rooted at the
 922 base of the Earth’s mantle beneath major hotspots. *Nature*, 525(7567), 95–99. doi:
 923 10.1038/nature14876
- 924 Fu, S., Yang, J., Tsujino, N., Okuchi, T., Purevjav, N., & Lin, J.-F. (2019). Single-
 925 crystal elasticity of (Al, Fe)-bearing bridgmanite and seismic shear wave radial
 926 anisotropy at the topmost lower mantle. *Earth and Planetary Science Letters*,
 927 518, 116–126.
- 928 Garnero, E. J., & Lay, T. (1997). Lateral variations in lowermost mantle shear
 929 wave anisotropy beneath the north Pacific and Alaska. *Journal Of Geophysical
 930 Research-Solid Earth*, 102(B4), 8121–8135. doi: 10.1029/96JB03830
- 931 Garnero, E. J., Maupin, V., Lay, T., & Fouch, M. J. (2004). Variable azimuthal
 932 anisotropy in Earth’s lowermost mantle. *Science*, 306(5694), 259–261. doi: 10
 933 .1126/science.1103411
- 934 Garnero, E. J., & McNamara, A. K. (2008). Structure and dynamics of Earth’s
 935 lower mantle. *Science*, 320(5876), 626–628. doi: 10.1126/science.1148028
- 936 Garnero, E. J., McNamara, A. K., & Shim, S.-H. (2016, June). Continent-sized
 937 anomalous zones with low seismic velocity at the base of Earth’s mantle. *Nature
 938 Geoscience*, 9(7), 481–489. doi: 10.1038/ngeo2733

- 939 Garnero, E. J., Revenaugh, J., Williams, Q., Lay, T., & Kellogg, L. (1998). Ul-
 940 tralow velocity zone at the core–mantle boundary. In M. Gurnis, M. E. Wysession,
 941 E. Knittle, & B. A. Buffett (Eds.), *The Core–Mantle Boundary Region* (pp. 319–
 942 334). Washington, D.C., USA: American Geophysical Union.
- 943 Girard, J., Amulele, G., Farla, R., Mohiuddin, A., & Karato, S.-i. (2016, January).
 944 Shear deformation of bridgmanite and magnesiowustite aggregates at lower mantle
 945 conditions. *Science*, *351*(6269), 144–147. doi: 10.1126/science.aad3113
- 946 Girard, J., Chen, J., & Raterron, P. (2012). Deformation of periclase single crys-
 947 tals at high pressure and temperature: Quantification of the effect of pressure on
 948 slip-system activities. *Journal of Applied Physics*, *111*(11), 112607.
- 949 Goryaeva, A. M., Carrez, P., & Cordier, P. (2015). Modeling defects and plastic-
 950 ity in MgSiO₃ post-perovskite: Part 2—Screw and edge [100] dislocations. *Physics
 951 and chemistry of minerals*, *42*(10), 793–803.
- 952 Goryaeva, A. M., Carrez, P., & Cordier, P. (2016). Low viscosity and high attenu-
 953 ation in MgSiO₃ post-perovskite inferred from atomic-scale calculations. *Scientific
 954 reports*, *6*, 34771.
- 955 Goryaeva, A. M., Carrez, P., & Cordier, P. (2017). Modeling defects and plastic-
 956 ity in MgSiO₃ post-perovskite: Part 3—Screw and edge [001] dislocations. *Physics
 957 and Chemistry of Minerals*, *44*(7), 521–533.
- 958 Grund, M., & Ritter, J. R. (2019). Widespread seismic anisotropy in Earth’s lower-
 959 most mantle beneath the Atlantic and Siberia. *Geology*, *47*(2), 123–126.
- 960 Hall, S. A., Kendall, J.-M., & Van der Baan, M. (2004). Some comments on the ef-
 961 fects of lower-mantle anisotropy on SKS and SKKS phases. *Physics of The Earth
 962 and Planetary Interiors*, *146*(3–4), 469–481. doi: 10.1016/j.pepi.2004.05.002
- 963 Hernlund, J., Thomas, C., & Tackley, P. J. (2005). A doubling of the post-
 964 perovskite phase boundary and structure of the Earth’s lowermost mantle. *Nature*,
 965 *434*(7035), 882–886. doi: 10.1038/nature03472
- 966 Hirose, K., Nagaya, Y., Merkel, S., & Ohishi, Y. (2010). Deformation of MnGeO₃
 967 post-perovskite at lower mantle pressure and temperature. *Geophysical Research
 968 Letters*, *37*(L20302), 1–5. doi: 10.1029/2010GL044977
- 969 Hirose, K., Wentzcovitch, R., Yuen, D., & Lay, T. (2015). Mineralogy of the deep
 970 mantle - The post-perovskite phase and its geophysical significance. *Treatise on
 971 Geophysics*, 85–115.

- 972 Hunt, S. A., Walker, A. M., & Mariani, E. (2016, May). In-situ measurement of tex-
 973 ture development rate in CaIrO₃ post-perovskite. *Physics of the Earth and Plane-*
 974 *tary Interiors*. doi: 10.1016/j.pepi.2016.05.007
- 975 Hunt, S. A., Weidner, D. J., Li, L., Wang, L., Walte, N. P., Brodholt, J. P., &
 976 Dobson, D. P. (2009). Weakening of calcium iridate during its transformation
 977 from perovskite to post-perovskite. *Nature Geoscience*, 2(11), 794-797. doi:
 978 10.1038/NGEO663
- 979 Iitaka, T., Hirose, K., Kawamura, K., & Murakami, M. (2004). The elasticity of
 980 the MgSiO₃ post-perovskite phase in the Earth's lowermost mantle. *Nature*,
 981 430(6998), 442-445. doi: 10.1038/nature02702
- 982 Jackson, J. M., Sinogeikin, S. V., Jacobsen, S. D., Reichmann, H. J., Mackwell,
 983 S. J., & Bass, J. D. (2006). Single-crystal elasticity and sound velocities of
 984 (Mg_{0.94}Fe_{0.06})O ferropericlasite to 20 GPa. *Journal of Geophysical Research: Solid*
 985 *Earth*, 111(B9).
- 986 Kaercher, P., Miyagi, L., Kanitpanyacharoen, W., Zepeda-Alarcon, E., Wang, Y.,
 987 Parkinson, D., . . . Wenk, H. (2016, December). Two-phase deformation of lower
 988 mantle mineral analogs. *Earth and Planetary Science Letters*, 456, 134-145. doi:
 989 10.1016/j.epsl.2016.09.030
- 990 Karato, S.-i. (1998). Some remarks on the origin of seismic anisotropy in the D''
 991 layer. *Earth Planets Space*, 50, 1019-1028.
- 992 Karki, B., Wentzcovitch, R., de Gironcoli, S., & Baroni, S. (2000). High-pressure lat-
 993 tice dynamics and thermoelasticity of MgO. *Physical Review B*, 61(13), 8793.
- 994 Kawai, K., & Geller, R. J. (2010). The vertical flow in the lowermost man-
 995 tle beneath the Pacific from inversion of seismic waveforms for anisotropic
 996 structure. *Earth and Planetary Science Letters*, 297(1-2), 190-198. doi:
 997 10.1016/j.epsl.2010.05.037
- 998 Kawakatsu, H. (2015). A new fifth parameter for transverse isotropy. *Geophysical*
 999 *Journal International*, 204(1), 682-685.
- 1000 Kendall, J.-M., & Silver, P. G. (1996). Constraints from seismic anisotropy on
 1001 the nature of the lowermost mantle. *Nature*, 381(6581), 409-412. doi: 10.1038/
 1002 381409a0
- 1003 Kendall, J.-M., & Silver, P. G. (1998). Investigating causes of D'' anisotropy. In *The*
 1004 *core-mantle boundary region* (p. 97-118). American Geophysical Union.

- 1005 Kennett, B. L. N., Engdahl, E., & Buland, R. (1995). Constraints on seismic ve-
 1006 locities in the Earth from travel-times. *Geophysical Journal International*, *122*(1),
 1007 108-124. doi: 10.1111/j.1365-246X.1995.tb03540.x
- 1008 Koelemeijer, P., Schuberth, B., Davies, D., Deuss, A., & Ritsema, J. (2018, July).
 1009 Constraints on the presence of post-perovskite in Earth's lowermost mantle from
 1010 tomographic-geodynamic model comparisons. *Earth and Planetary Science Let-*
 1011 *ters*, *494*, 226-238. doi: 10.1016/j.epsl.2018.04.056
- 1012 Koelemeijer, P. J., Deuss, A., & Trampert, J. (2012). Normal mode sensitiv-
 1013 ity to earth's D'' layer and topography on the core-mantle boundary: what we
 1014 can and cannot see. *Geophysical Journal International*, *190*(1), 553-568. doi:
 1015 10.1111/j.1365-246X.2012.05499.x
- 1016 Komatitsch, D., & Tromp, J. (2002). Spectral-element simulations of global seismic
 1017 wave propagation - I. Validation. *Geophysical Journal International*, *149*(2), 390-
 1018 412.
- 1019 Komatitsch, D., Tsuboi, S., Ji, C., & Tromp, J. (2003). A 14.6 billion degrees
 1020 of freedom, 5 teraflops, 2.5 terabyte earthquake simulation on the Earth Sim-
 1021 ulator. *Proceedings of the ACM/IEEE SC2003 Conference (SC'03)*, 1-8. doi:
 1022 10.1145/1048935.1050155
- 1023 Komatitsch, D., Vinnik, L. P., & Chevrot, S. (2010). SHdiff-SVdiff splitting in an
 1024 isotropic Earth. *Journal Of Geophysical Research-Solid Earth*, *115*, B07312. doi:
 1025 10.1029/2009JB006795
- 1026 Krischer, L., Megies, T., Barsch, R., Beyreuther, M., Lecocq, T., Caudron, C., &
 1027 Wassermann, J. (2015). Obspy: A bridge for seismology into the scientific Python
 1028 ecosystem. *Computational Science & Discovery*, *8*(1), 014003.
- 1029 Lay, T., & Young, C. (1991). Analysis of seismic SV waves in the core's penumbra.
 1030 *Geophysical Research Letters*, *18*(8), 1373-1376. doi: 10.1029/91GL01691
- 1031 Lebensohn, R., & Tomé, C. (1993). A self-consistent anisotropic approach for
 1032 the simulation of plastic-deformation and texture development of polycrystals—
 1033 application to zirconium alloys. *Acta Metallurgica Et Materialia*, *41*(9), 2611–
 1034 2624. doi: 10.1016/0956-7151(93)90130-K
- 1035 Lekić, V., Cottaar, S., Dziewoński, A., & Romanowicz, B. (2012, December). Cluster
 1036 analysis of global lower mantle tomography: A new class of structure and implica-
 1037 tions for chemical heterogeneity. *Earth and Planetary Science Letters*, *357-358*,

- 1038 68-77. doi: 10.1016/j.epsl.2012.09.014
- 1039 Li, L., Brodholt, J. P., Stackhouse, S., Weidner, D. J., Alfredsson, M., & Price,
1040 G. D. (2005). Elasticity of (Mg, Fe)(Si, Al)O₃-perovskite at high pressure. *Earth
1041 and Planetary Science Letters*, 240(2), 529–536.
- 1042 Li, L., Weidner, D. J., Brodholt, J. P., Alfé, D., Price, G. D., Caracas, R., & Wentz-
1043 covitch, R. M. (2006). Elasticity of {CaSiO}₃ perovskite at high pressure
1044 and high temperature. *Physics of The Earth and Planetary Interiors*, 155(3-4),
1045 249-259. doi: 10.1016/j.pepi.2005.12.006
- 1046 Lin, J.-F., Wenk, H.-R., Voltolini, M., Speziale, S., Shu, J., & Duffy, T. S. (2009).
1047 Deformation of lower-mantle ferropericlasite (Mg, Fe)O across the electronic spin
1048 transition. *Physics and Chemistry of Minerals*, 36(10), 585.
- 1049 Long, M. (2009). Complex anisotropy in D'' beneath the eastern pacific from SKS-
1050 SKKS splitting discrepancies. *Earth and Planetary Science Letters*, 283(1-4), 181-
1051 189. doi: 10.1016/j.epsl.2009.04.019
- 1052 Long, M. D., & Lynner, C. (2015, September). Seismic anisotropy in the lowermost
1053 mantle near the Perm Anomaly. *Geophysical Research Letters*, 42(17), 7073-7080.
1054 doi: 10.1002/2015GL065506
- 1055 Lynner, C., & Long, M. D. (2014, May). Lowermost mantle anisotropy and defor-
1056 mation along the boundary of the African LLSVP. *Geophysical Research Letters*,
1057 41(10), 3447-3454. doi: 10.1002/2014GL059875
- 1058 Madi, K., Forest, S., Cordier, P., & Boussuge, M. (2005). Numerical study of creep
1059 in two-phase aggregates with a large rheology contrast: Implications for the lower
1060 mantle. *Earth and Planetary Science Letters*, 237(1-2), 223–238.
- 1061 Mainprice, D. (2007). Seismic anisotropy of the deep Earth from a mineral and rock
1062 physics perspective. In *Treatise on Geophysics* (p. 437-491). Elsevier. doi: 10
1063 .1016/B978-044452748-6.00045-6
- 1064 Mainprice, D., Tommasi, A., Ferr e, D., Carrez, P., & Cordier, P. (2008). Pre-
1065 dicted glide systems and crystal preferred orientations of polycrystalline silicate
1066 Mg-Perovskite at high pressure: Implications for the seismic anisotropy in the
1067 lower mantle. *Earth and Planetary Science Letters*, 271(1-4), 135-144. doi:
1068 10.1016/j.epsl.2008.03.058
- 1069 Mancinelli, N. J., & Shearer, P. M. (2013). Reconciling discrepancies among esti-
1070 mates of small-scale mantle heterogeneity from PKP precursors. *Geophysical Jour-*

- 1071 *nal International*, 195(3), 1721–1729.
- 1072 Marquardt, H., Speziale, S., Reichmann, H. J., Frost, D. J., & Schilling, F. R.
 1073 (2009). Single-crystal elasticity of $(\text{Mg}_{0.9}\text{Fe}_{0.1})\text{O}$ to 81 GPa. *Earth and Plane-*
 1074 *tary Science Letters*, 287(3-4), 345-352. doi: 10.1016/j.epsl.2009.08.017
- 1075 Matzel, E., Sen, M., & Grand, S. (1996). Evidence for anisotropy in the deep mantle
 1076 beneath Alaska. *Geophysical Research Letters*, 23(18), 2417-2420. doi: 10.1029/
 1077 96GL02186
- 1078 Maupin, V. (1994). On the possibility of anisotropy in the D'' layer as inferred from
 1079 the polarization of diffracted S waves. *Physics of The Earth and Planetary Interi-*
 1080 *ors*, 87(1-2), 1-32. doi: 10.1016/0031-9201(94)90019-1
- 1081 Maupin, V., Garnero, E. J., Lay, T., & Fouch, M. J. (2005). Azimuthal anisotropy
 1082 in the D'' layer beneath the Caribbean. *Journal Of Geophysical Research-Solid*
 1083 *Earth*, 110(B8), B08301. doi: 10.1029/2004JB003506
- 1084 McDonough, W., & Sun, S. (1995). The composition of the Earth. *Chemical Geol-*
 1085 *ogy*, 120(3-4), 223-253.
- 1086 Merkel, S., McNamara, A. K., Kubo, A., Speziale, S., Miyagi, L., Meng, Y., ...
 1087 Wenk, H.-R. (2007). Deformation of $(\text{Mg,Fe})\text{SiO}_3$ post-perovskite and D''
 1088 anisotropy. *Science*, 316(5832), 1729-1732. doi: 10.1126/science.1140609
- 1089 Merkel, S., Wenk, H.-R., Shu, J., Shen, G., Gillet, P., Mao, H., & Hemley, R. (2002).
 1090 Deformation of polycrystalline MgO at pressures of the lower mantle. *Journal Of*
 1091 *Geophysical Research-Solid Earth*, 107(B11), 2271. doi: 10.1029/2001JB000920
- 1092 Miyagi, L., Kanitpanyacharoen, W., Kaercher, P., Lee, K. K. M., & Wenk, H.-R.
 1093 (2010). Slip systems in MgSiO_3 post-perovskite: Implications for D'' anisotropy.
 1094 *Science*, 329(5999), 1639-1641. doi: 10.1126/science.1192465
- 1095 Miyagi, L., Kanitpanyacharoen, W., Stackhouse, S., Militzer, B., & Wenk, H.-R.
 1096 (2011). The enigma of post-perovskite anisotropy: Deformation versus trans-
 1097 formation textures. *Physics And Chemistry Of Minerals*, 38(9), 665-678. doi:
 1098 10.1007/s00269-011-0439-y
- 1099 Miyagi, L., Merkel, S., Yagi, T., Sata, N., Ohishi, Y., & Wenk, H.-R. (2009,
 1100 May). Diamond anvil cell deformation of CaSiO_3 perovskite up to 49 GPa.
 1101 *Physics of the Earth and Planetary Interiors*, 174(1-4), 159–164. doi: 10.1016/
 1102 j.pepi.2008.05.018
- 1103 Miyagi, L., & Wenk, H.-R. (2016). Texture development and slip systems in bridg-

- 1104 manite and bridgmanite + ferropericlasite aggregates. *Physics and Chemistry of*
 1105 *Minerals*, 43(8), 597–613.
- 1106 Moulik, P., & Ekstrom, G. (2014, oct). An anisotropic shear velocity model of the
 1107 Earth’s mantle using normal modes, body waves, surface waves and long-period
 1108 waveforms. *Geophys. J. Int.*, 199(3), 1713–1738. doi: 10.1093/gji/ggu356
- 1109 Murakami, M., Hirose, K., Kawamura, K., Sata, N., & Ohishi, Y. (2004). Post-
 1110 perovskite phase transition in MgSiO₃. *Science*, 304(5672), 855-858. doi: 10.1126/
 1111 science.1095932
- 1112 Nakagawa, T., & Tackley, P. J. (2011). Effects of low-viscosity post-perovskite on
 1113 thermo-chemical mantle convection in a 3-D spherical shell. *Geophysical research*
 1114 *letters*, 38(4).
- 1115 Nisr, C., Ribárik, G., Ungar, T., Vaughan, G. B. M., Cordier, P., & Merkel, S.
 1116 (2012). High resolution three-dimensional X-ray diffraction study of dislocations in
 1117 grains of MgGeO₃ post-perovskite at 90 GPa. *Journal Of Geophysical Research*,
 1118 117(B3), B03201. doi: 10.1029/2011JB008401
- 1119 Niu, F., & Perez, A. (2004). Seismic anisotropy in the lower mantle: A comparison
 1120 of waveform splitting of SKS and SKKS. *Geophysical Research Letters*, 31(24),
 1121 L24612. doi: 10.1029/2004GL021196
- 1122 Niwa, K., Miyajima, N., Seto, Y., Ohgushi, K., Gotou, H., & Yagi, T. (2012). In situ
 1123 observation of shear stress-induced perovskite to post-perovskite phase transition
 1124 in CaIrO₃ and the development of its deformation texture in a diamond-anvil cell
 1125 up to 30 GPa. *Physics of The Earth and Planetary Interiors*, 194-195(C), 10-17.
 1126 doi: 10.1016/j.pepi.2012.01.007
- 1127 Nowacki, A., Walker, A. M., Wookey, J., & Kendall, J.-M. (2013). Evaluating post-
 1128 perovskite as a cause of D'' anisotropy in regions of palaeosubduction. *Geophysical*
 1129 *Journal International*, 192(3), 1085-1090. doi: 10.1093/gji/ggs068
- 1130 Nowacki, A., & Wookey, J. (2016, September). The limits of ray theory when mea-
 1131 suring shear wave splitting in the lowermost mantle with ScS waves. *Geophysical*
 1132 *Journal International*, 207, 1573-1583. doi: 10.1093/gji/ggw358
- 1133 Nowacki, A., Wookey, J., & Kendall, J.-M. (2010). Deformation of the lowermost
 1134 mantle from seismic anisotropy. *Nature*, 467(7319), 1091-1095. doi: 10.1038/
 1135 nature09507
- 1136 Nowacki, A., Wookey, J., & Kendall, J.-M. (2011). New advances in using seis-

- 1137 mic anisotropy, mineral physics and geodynamics to understand deformation
 1138 in the lowermost mantle. *Journal of Geodynamics*, 52(3-4), 205-228. doi:
 1139 10.1016/j.jog.2011.04.003
- 1140 Oganov, A., Brodholt, J. P., & Price, G. D. (2001). The elastic constants of
 1141 MgSiO₃ perovskite at pressures and temperatures of the Earth's mantle. *Nature*,
 1142 411(6840), 934-937. doi: 10.1038/35082048
- 1143 Oganov, A., & Ono, S. (2004). Theoretical and experimental evidence for a post-
 1144 perovskite phase of MgSiO₃ in Earth's D'' layer. *Nature*, 430(6998), 445-448. doi:
 1145 10.1038/nature02701
- 1146 Panning, M., Lekić, V., & Romanowicz, B. (2010). Importance of crustal correc-
 1147 tions in the development of a new global model of radial anisotropy. *Journal Of*
 1148 *Geophysical Research-Solid Earth*, 115, B12325. doi: 10.1029/2010JB007520
- 1149 Parisi, L., Ferreira, A. M. G., & Ritsema, J. (2018, May). Apparent splitting of S
 1150 waves propagating through an isotropic lowermost mantle. *Journal of Geophysical*
 1151 *Research: Solid Earth*, 123(5), 3909-3922. doi: 10.1002/2017JB014394
- 1152 Pisconti, A., Thomas, C., & Wookey, J. (2019, May). Discriminating between causes
 1153 of D'' anisotropy using reflections and splitting measurements for a single path.
 1154 *Journal of Geophysical Research: Solid Earth*. doi: 10.1029/2018JB016993
- 1155 Ranganathan, S. I., & Ostojja-Starzewski, M. (2008). Universal elastic anisotropy
 1156 index. *Physical Review Letters*, 101(5), 055504. doi: 10.1103/PhysRevLett.101
 1157 .055504
- 1158 Reali, R., Van Orman, J. A., Pigott, J. S., Jackson, J. M., Bovioli, F., Carrez, P., &
 1159 Cordier, P. (2019). The role of diffusion-driven pure climb creep on the rheology
 1160 of bridgmanite under lower mantle conditions. *Scientific reports*, 9(1), 2053.
- 1161 Reiss, M., Long, M., & Creasy, N. (2019). Lowermost mantle anisotropy beneath
 1162 Africa from differential SKS-SKKS shear-wave splitting. *Journal of Geophysical*
 1163 *Research: Solid Earth*. doi: 10.1029/2018JB017160
- 1164 Romanowicz, B., & Wenk, H.-R. (2017, August). Anisotropy in the deep Earth.
 1165 *Physics of the Earth and Planetary Interiors*, 269, 58-90. doi: 10.1016/j.pepi.2017
 1166 .05.005
- 1167 Silver, P. G., & Chan, W. W. (1991). Shear-wave splitting and subcontinental
 1168 mantle deformation. *Journal Of Geophysical Research-Solid Earth*, 96(B10),
 1169 16429-16454. doi: 10.1029/91JB00899

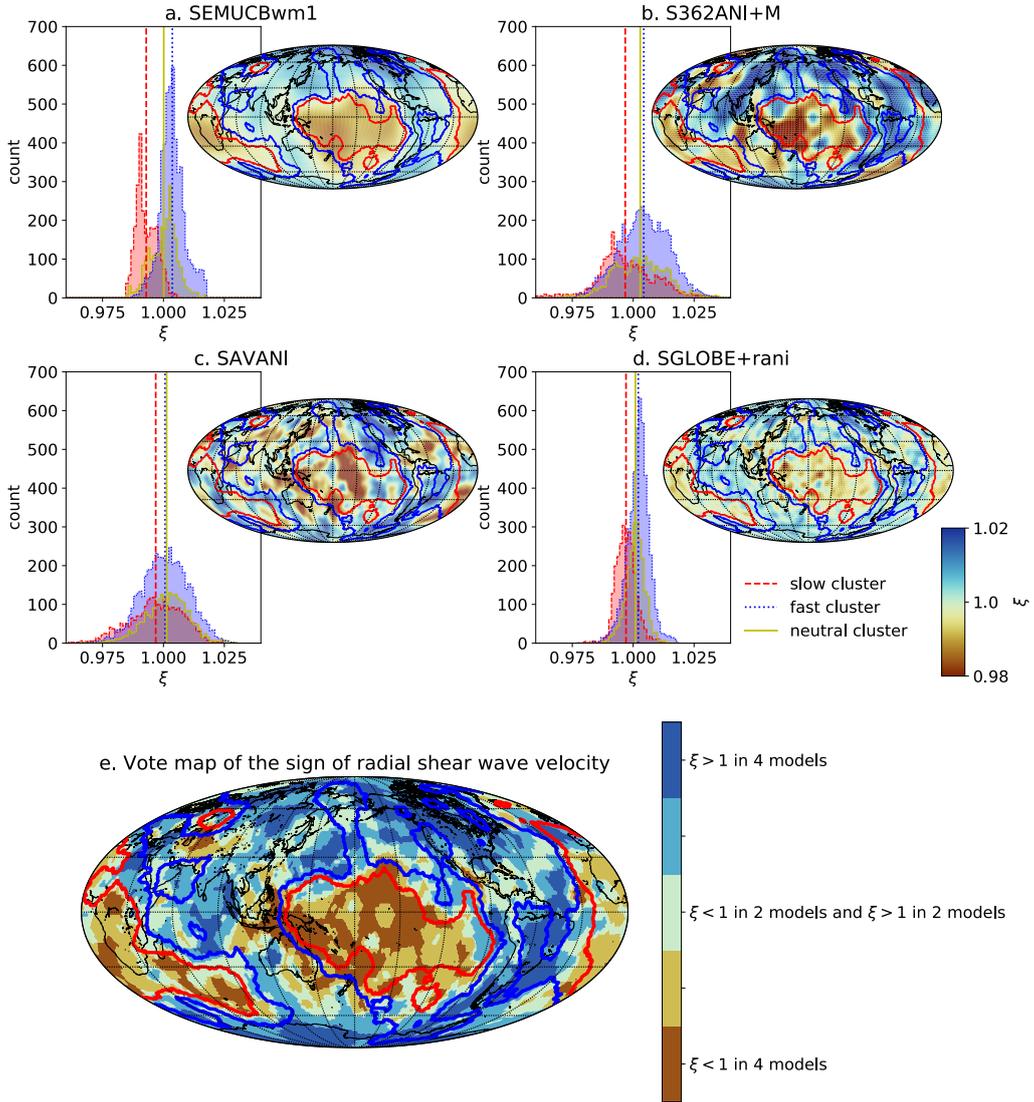
- 1170 Simmons, N. A., Forte, A. M., & Grand, S. (2009). Joint seismic, geodynamic
 1171 and mineral physical constraints on three-dimensional mantle heterogene-
 1172 ity: Implications for the relative importance of thermal versus compositional
 1173 heterogeneity. *Geophysical Journal International*, *177*(3), 1284-1304. doi:
 1174 10.1111/j.1365-246X.2009.04133.x
- 1175 Soldati, G., Boschi, L., & Piersanti, A. (2003). Outer core density heterogeneity and
 1176 the discrepancy between PKP and PcP travel time observations. *Geophysical Re-*
 1177 *search Letters*, *30*(4), 1190. doi: 10.1029/2002GL016647
- 1178 Stackhouse, S., Brodholt, J. P., & Price, G. D. (2005). High temperature elastic
 1179 anisotropy of the perovskite and post-perovskite Al_2O_3 . *Geophysical Research Let-*
 1180 *ters*, *32*(13), L13305. doi: 10.1029/2005GL023163
- 1181 Stackhouse, S., Brodholt, J. P., Wookey, J., Kendall, J.-M., & Price, G. D. (2005).
 1182 The effect of temperature on the seismic anisotropy of the perovskite and post-
 1183 perovskite polymorphs of MgSiO_3 . *Earth and Planetary Science Letters*, *230*(1-2),
 1184 1-10. doi: 10.1016/j.epsl.2004.11.021
- 1185 Sun, N., Shi, W., Mao, Z., Zhou, C., & Prakapenka, V. B. (2019, December). High
 1186 pressure-temperature study on the thermal equations of state of seifertite and
 1187 CaCl_2 -type SiO_2 . *Journal of Geophysical Research: Solid Earth*, *124*(12), 12620–
 1188 12630. doi: 10.1029/2019JB017853
- 1189 Tesoniero, A., Cammarano, F., & Boschi, L. (2016, July). S-to-P heterogeneity ratio
 1190 in the lower mantle and thermo-chemical implications. *Geochemistry, Geophysics,*
 1191 *Geosystems*, *17*(7), 2522-2538. doi: 10.1002/2016GC006293
- 1192 Thomas, C., Wookey, J., Brodholt, J. P., & Fieseler, T. (2011). Anisotropy as
 1193 cause for polarity reversals of D'' reflections. *Earth and Planetary Science Letters*,
 1194 *307*(3-4), 369-376. doi: 10.1016/j.epsl.2011.05.011
- 1195 Thomas, C., Wookey, J., & Simpson, M. (2007). D'' anisotropy beneath Southeast
 1196 Asia. *Geophysical Research Letters*, *34*(4), L04301. doi: 10.1029/2006GL028965
- 1197 Thomson, A. R., Crichton, W. A., Brodholt, J. P., Wood, I. G., Siersch, N. C., Muir,
 1198 J. M. R., ... Hunt, S. A. (2019, August). Seismic velocities of CaSiO_3 perovskite
 1199 can explain LLSVPs in Earth's lower mantle. *Nature*, *572*(7771), 643-647. doi:
 1200 10.1038/s41586-019-1483-x
- 1201 Tommasi, A., Goryaeva, A., Carrez, P., Cordier, P., & Mainprice, D. (2018,
 1202 June). Deformation, crystal preferred orientations, and seismic anisotropy in

- 1203 the Earth's D'' layer. *Earth and Planetary Science Letters*, *492*, 35-46. doi:
1204 10.1016/j.epsl.2018.03.032
- 1205 Tsuchiya, T., Tsuchiya, J., Umemoto, K., & Wentzcovitch, R. M. (2004). Phase
1206 transition in MgSiO₃ perovskite in the earth's lower mantle. *Earth and Planetary
1207 Science Letters*, *224*(3-4), 241-248. doi: 10.1016/j.epsl.2004.05.017
- 1208 Tsujino, N., Nishihara, Y., Yamazaki, D., Seto, Y., Higo, Y., & Takahashi, E. (2016,
1209 October). Mantle dynamics inferred from the crystallographic preferred orienta-
1210 tion of bridgmanite. *Nature*, *539*(7627), 81-84. doi: 10.1038/nature19777
- 1211 Vinnik, L. P., Breger, L., & Romanowicz, B. (1998). Anisotropic structures at the
1212 base of the Earth's mantle. *Nature*, *393*(6685), 564-567. doi: 10.1038/31208
- 1213 Walker, A. M., Carrez, P., & Cordier, P. (2010). Atomic-scale models of disloca-
1214 tion cores in minerals: Progress and prospects. *Mineralogical Magazine*, *74*(3),
1215 381-413. doi: 10.1180/minmag.2010.074.3.381
- 1216 Walker, A. M., Dobson, D. P., Wookey, J., Nowacki, A., & Forte, A. M. (2018). The
1217 anisotropic signal of topotaxy during phase transitions in D''. *Physics of the Earth
1218 and Planetary Interiors*, *276*, 159-171. doi: 10.1016/j.pepi.2017.05.013
- 1219 Walker, A. M., Forte, A. M., Wookey, J., Nowacki, A., & Kendall, J.-M. (2011).
1220 Elastic anisotropy of D'' predicted from global models of mantle flow. *Geochem-
1221 istry Geophysics Geosystems*, *12*(10), Q10006. doi: 10.1029/2011GC003732
- 1222 Walker, A. M., & Wookey, J. (2012). MSAT—A new toolkit for the analysis of elas-
1223 tic and seismic anisotropy. *Computers & Geosciences*, *49*, 81-90. doi: 10.1016/j
1224 .cageo.2012.05.031
- 1225 Walpole, J., Wookey, J., Kendall, J.-M., & Masters, T.-G. (2017). Seismic anisotropy
1226 and mantle flow below subducting slabs. *Earth and Planetary Science Letters*,
1227 *465*, 155-167.
- 1228 Walsh, E., Arnold, R., & Savage, M. K. (2013, October). Silver and Chan revisited.
1229 *Journal of Geophysical Research: Solid Earth*, *118*(10), 5500-5515. doi: 10.1002/
1230 jgrb.50386
- 1231 Walte, N. P., Heidelbach, F., Miyajima, N., Frost, D. J., Rubie, D. C., & Dobson,
1232 D. P. (2009). Transformation textures in post-perovskite: Understanding mantle
1233 flow in the D'' layer of the Earth. *Geophysical Research Letters*, *36*, L04302. doi:
1234 10.1029/2008GL036840
- 1235 Wang, Y., Hilaret, N., Nishiyama, N., Yahata, N., Tsuchiya, T., Morard, G., &

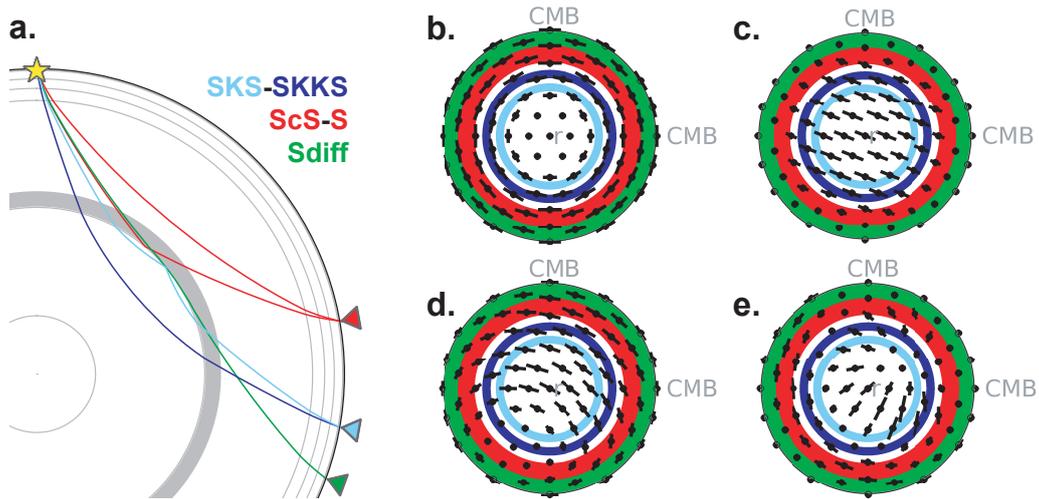
- 1236 Fiquet, G. (2013). High-pressure, high-temperature deformation of CaGeO_3
 1237 (perovskite) \pm MgO aggregates: Implications for multiphase rheology of the lower
 1238 mantle. *Geochemistry, Geophysics, Geosystems*, *14*(9), 3389–3408.
- 1239 Wang, Y., & Wen, L. (2007). Complex seismic anisotropy at the border of a very
 1240 low velocity province at the base of the Earth’s mantle. *Journal Of Geophysical*
 1241 *Research-Solid Earth*, *112*(B9), B09305. doi: 10.1029/2006JB004719
- 1242 Wenk, H.-R., Cottaar, S., Tomé, C. N., McNamara, A. K., & Romanowicz, B.
 1243 (2011). Deformation in the lowermost mantle: From polycrystal plasticity to
 1244 seismic anisotropy. *Earth and Planetary Science Letters*, *306*(1-2), 33-45. doi:
 1245 10.1016/j.epsl.2011.03.021
- 1246 Wenk, H.-R., Lonardeli, I., Pehl, J., Devine, J., Prakapenka, V., Shen, G., & Mao,
 1247 H.-K. (2004). In situ observation of texture development in olivine, ringwoodite,
 1248 magnesiowüstite and silicate perovskite at high pressure. *Earth and Planetary*
 1249 *Science Letters*, *226*(3), 507-519. doi: 10.1016/j.epsl.2004.07.033
- 1250 Wentzcovitch, R. M., Tsuchiya, T., & Tsuchiya, J. (2006). MgSiO_3 postperovskite at
 1251 D'' conditions. *Proceedings Of The National Academy Of Sciences Of The United*
 1252 *States Of America*, *103*(3), 543-546. doi: 10.1073/pnas.0506879103
- 1253 Wheeler, J. (2009, September). The preservation of seismic anisotropy in the Earth’s
 1254 mantle during diffusion creep. *Geophysical Journal International*, *178*(3), 1723-
 1255 1732. doi: 10.1111/j.1365-246X.2009.04241.x
- 1256 Wheeler, J. (2010, July). Anisotropic rheology during grain boundary diffusion
 1257 creep and its relation to grain rotation, grain boundary sliding and superplasticity.
 1258 *Philosophical Magazine*, *90*(21), 2841-2864. doi: 10.1080/14786431003636097
- 1259 Wolf, J., Creasy, N., Pisconti, A., Long, M. D., & Thomas, C. (2019). An investi-
 1260 gation of seismic anisotropy in the lowermost mantle beneath iceland. *Geophysical*
 1261 *Journal International*. doi: 10.1093/gji/ggz312
- 1262 Wookey, J., & Dobson, D. P. (2008). Between a rock and a hot place: The core-
 1263 mantle boundary. *Philosophical Transactions Of The Royal Society Of London*
 1264 *Series A-Mathematical Physical And Engineering Sciences*, *366*(1885), 4543-4557.
 1265 doi: 10.1098/rsta.2008.0184
- 1266 Wookey, J., & Kendall, J.-M. (2007). Seismic anisotropy of post-perovskite and the
 1267 lowermost mantle. In K. Hirose, J. Brodholt, T. Lay, & D. A. Yuen (Eds.), *Post-*
 1268 *perovskite: The last mantle phase transition* (pp. 171–189). Washington, D.C.,

- 1269 USA: American Geophysical Union Geophysical Monograph 174.
- 1270 Wookey, J., & Kendall, J.-M. (2008). Constraints on lowermost mantle mineralogy
1271 and fabric beneath Siberia from seismic anisotropy. *Earth and Planetary Science*
1272 *Letters*, *275*(1-2), 32-42. doi: 10.1016/j.epsl.2008.07.049
- 1273 Wookey, J., Kendall, J.-M., & Rumpker, G. (2005). Lowermost mantle anisotropy
1274 beneath the north Pacific from differential S–ScS splitting. *Geophysical Journal*
1275 *International*, *161*(3), 829-838. doi: 10.1111/j.1365-246X.2005.02623.x
- 1276 Wu, X., Lin, J.-F., Kaercher, P., Mao, Z., Liu, J., Wenk, H.-R., & Prakapenka, V. B.
1277 (2017). Seismic anisotropy of the D'' layer induced by (001) deformation of post-
1278 perovskite. *Nature Communications*, *8*, 14669.
- 1279 Wu, Z., Justo, J. F., & Wentzcovitch, R. M. (2013). Elastic anomalies in a spin-
1280 crossover system: Ferropicrinite at lower mantle conditions. *Physical review let-*
1281 *ters*, *110*(22), 228501.
- 1282 Wuestefeld, A., Al-Harrasi, O., Verdon, J. P., Wookey, J., & Kendall, J.-M. (2010).
1283 A strategy for automated analysis of passive microseismic data to image seismic
1284 anisotropy and fracture characteristics. *Geophysical Prospecting*, *58*(5), 753-771.
1285 doi: 10.1111/j.1365-2478.2010.00891.x
- 1286 Yamazaki, D., & Karato, S. (2007). Lattice-preferred orientation of lower man-
1287 tle materials and seismic anisotropy in the D'' layer. In *Post-perovskite: The last*
1288 *mantle phase transition* (pp. 69–78). Washington, D.C., USA: American Geophys-
1289 ical Union.
- 1290 Yamazaki, D., & Karato, S.-i. (2002). Fabric development in (Mg,Fe)O during large
1291 strain, shear deformation: implications for seismic anisotropy in Earth's lower
1292 mantle. *Physics of The Earth and Planetary Interiors*, *131*(3-4), 251-267. doi:
1293 10.1016/S0031-9201(02)00037-7
- 1294 Yamazaki, D., Yoshino, T., Ohfuji, H., Ando, J.-i., & Yoneda, A. (2006). Origin of
1295 seismic anisotropy in the D'' layer inferred from shear deformation experiments on
1296 post-perovskite phase. *Earth and Planetary Science Letters*, *252*(3-4), 372-378.
1297 doi: 10.1016/j.epsl.2006.10.004
- 1298 Young, C. J., & Lay, T. (1990). Multiple phase analysis of the shear velocity struc-
1299 ture in the D'' region beneath Alaska. *Journal of Geophysical Research: Solid*
1300 *Earth*, *95*(B11), 17385–17402.
- 1301 Yu, S., & Garnero, E. J. (2018). Ultra-low velocity zone locations: A global assess-

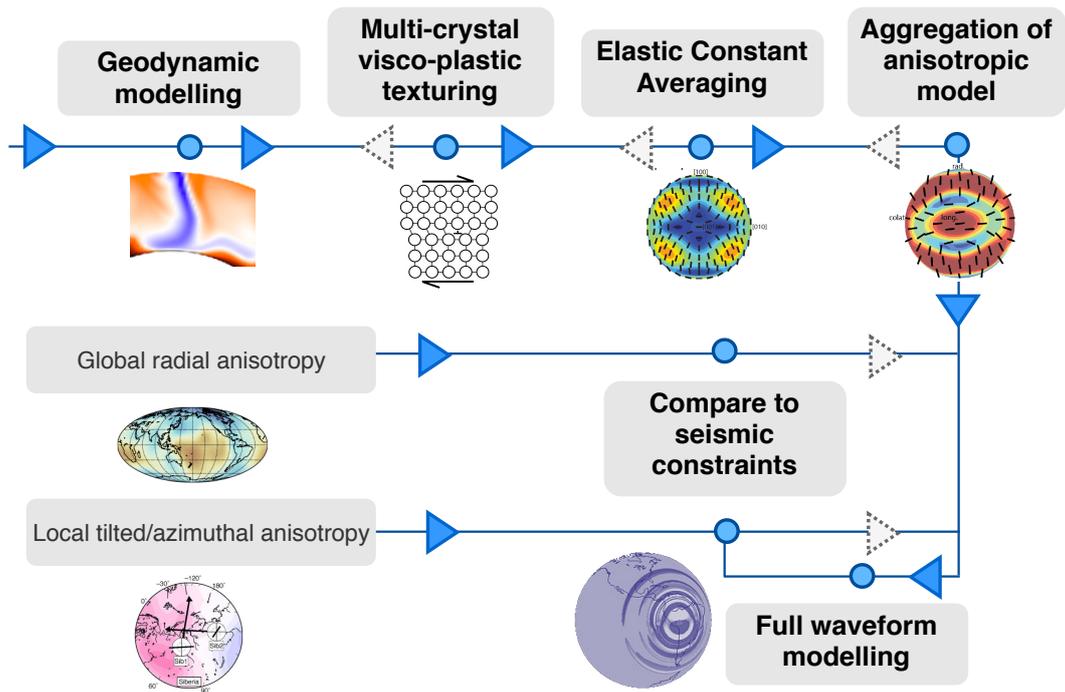
- 1302 ment. *Geochemistry, Geophysics, Geosystems*, 19(2), 396–414.
- 1303 Zhang, S., Cottaar, S., Liu, T., Stackhouse, S., & Militzer, B. (2016). High-pressure,
1304 temperature elasticity of Fe- and Al-bearing MgSiO₃: Implications for the Earth's
1305 lower mantle. *Earth and Planetary Science Letters*, 434, 264–273.
- 1306 Zhong, S., Zuber, M. T., Moresi, L., & Gurnis, M. (2000). Role of temperature-
1307 dependent viscosity and surface plates in spherical shell models of mantle convec-
1308 tion. *Journal of Geophysical Research: Solid Earth*, 105(B5), 11063–11082.



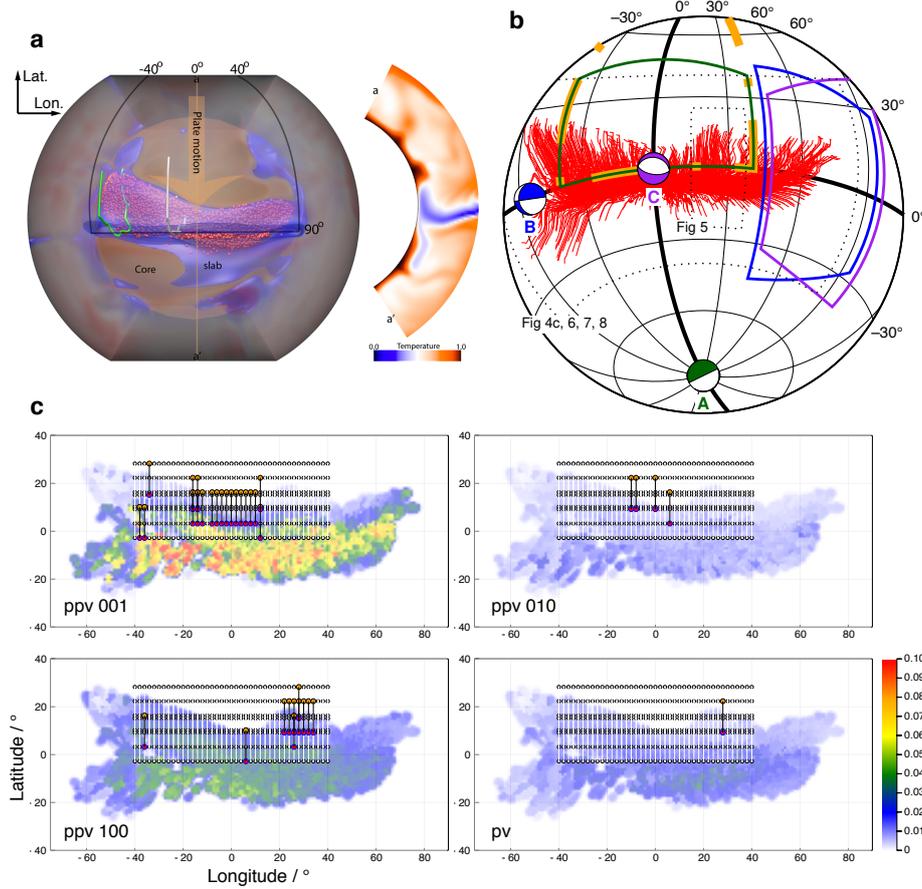
95 **Figure 1.** a. -d. Maps show shear wave radial anisotropic parameter ξ at 2800 km depth
 96 for SEMUCBwm1 (French and Romanowicz, 2014), S362ANI+M (Moulik and Ekstrom 2014),
 97 SAVANI (Auer et al. 2014), SGLOBE-rani (Chang et al., 2015). Red and blue contours show
 98 bounds at three votes for the isotropic slow and fast cluster based on votes across five isotropic
 99 models (Cottaar & Lekić, 2016). Histograms show distribution and mean values of ξ in the differ-
 100 ent cluster vote areas, red-'slow', blue-'fast', yellow-'neutral' (boundaries for 'neutral' cluster are
 101 not shown on the maps). e. Vote map showing where models agree on $\xi > 1$ or $\xi < 1$ (V_{SH} or
 102 V_{SV} being faster, respectively). All models agree that $\xi > 1$ for 18% of the map, while for $\xi < 1$
 103 the area is 13%.



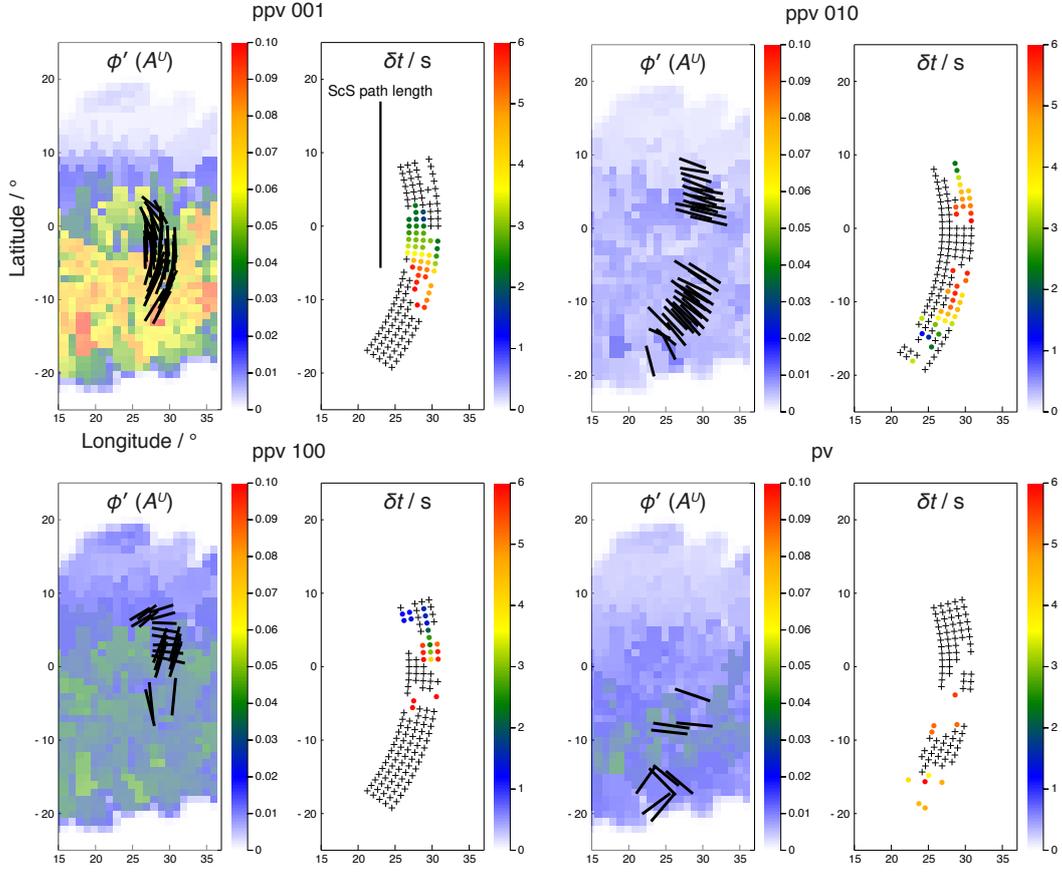
201 **Figure 2.** a. Ray paths for general body wave (pairs) used to constrain lowermost mantle
 202 anisotropy: SKS-SKKS (blue), ScS-S (red), S_{diff} (green) (made with Obspy; Krischer et al.,
 203 2015). b.-e. Hemisphere projections of various assumed anisotropic symmetries viewed from
 204 above (made with MSAT; Walker & Wookey, 2012). Bars show splitting direction and bar
 205 lengths show splitting strength as a function of shear wave propagation direction. Coloured shad-
 206 ing shows general sensitivity of body waves (see a.) although there is some overlap. b. Radial
 207 anisotropy with $\xi = 1.03$ c. 3% azimuthal anisotropy with a fast axis direction of 112° . d. Tilted
 208 anisotropy, i.e. anisotropy in c. tilted by 40° . e. Full anisotropic tensor for 75% post-perovskite
 209 and 25% periclase in a downgoing slab (see Section 4.2).



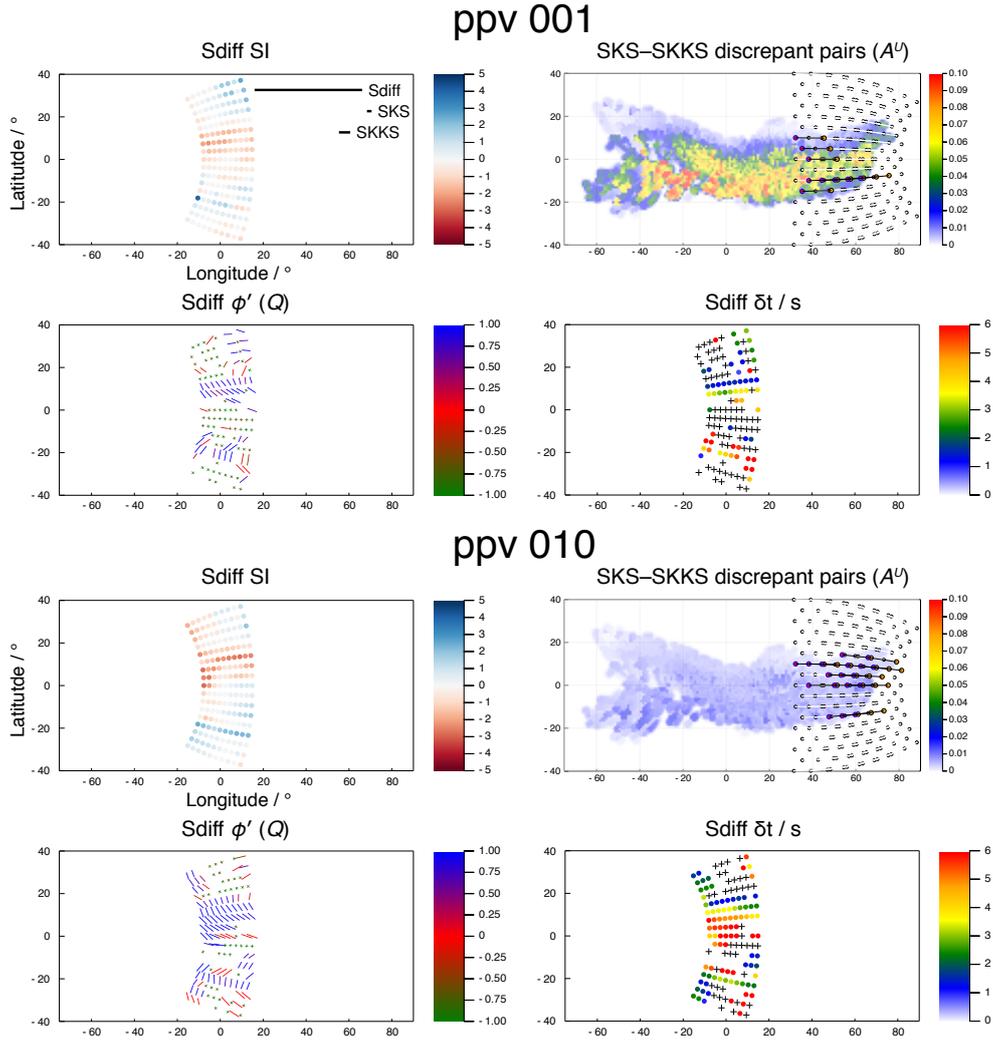
235 **Figure 3.** Showing the general steps in forward modelling from a flow model to interpreting
 236 seismic observations following the filled blue arrows as discussed in Section 3 . Dashed arrows
 237 indicate the inverse steps to go from seismic observations to flow directions, for which challenges
 238 and limitations are discussed in Section 5



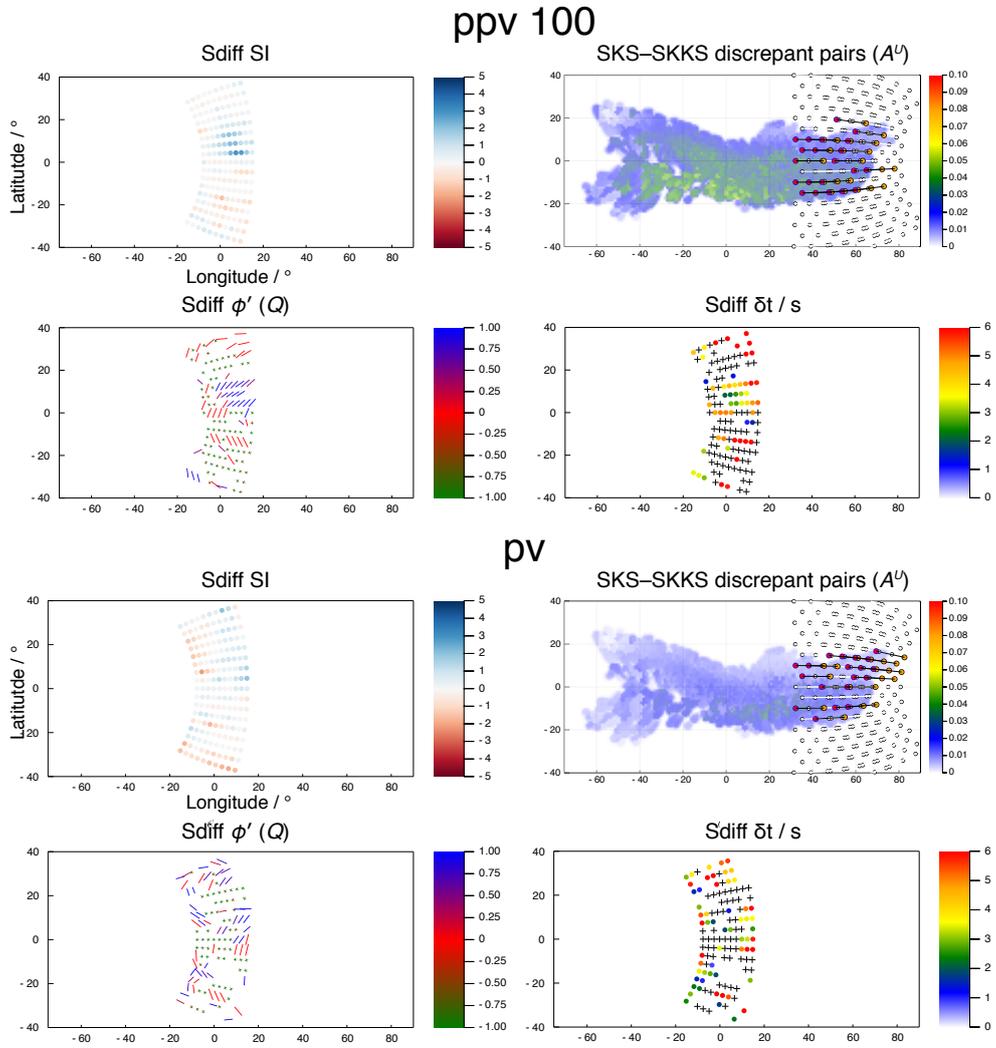
545 **Figure 4.** (a) Geodynamical setup of forward calculation, taken from Figure 1 of Cottaar et
 546 al. (2014). A slab is imposed, moving from north to south, which subducts along the equator.
 547 Tracer particles are shown by orange dots, with the path for two highlighted as green and white
 548 lines. Section a–a’ along longitude 0° to the right shows non-dimensional temperature. (b) Ge-
 549 ometry of synthetic seismic sources and receivers in relation to the slab model. Sources are shown
 550 by colour-coded lower-hemisphere focal mechanisms (annotated with the code in Table 1), match-
 551 ing the receiver locations, shown by open areas with solid boundaries. Red lines show the paths
 552 of tracer particles, and orange dash-dotted lines show the slab edges in panel (a). Areas shown
 553 by other figures are indicated by dotted black lines and labelled. (c) Discrepant SKS-SKKS split-
 554 ting for path ‘A’ (Table 1) for each plasticity model. Red and orange circles respectively show
 555 the core piercing points for SKKS and SKS waves for pairs which are discrepant, whilst white
 556 circles denote the piercing points of pairs which are not. Underlying colour shows the strength of
 557 anisotropy at the bottom of the slab texture model, using the universal elastic anisotropy index,
 558 A^U (Ranganathan & Ostoja-Starzewski, 2008) according to the colour scale on the bottom right.
 559 (For approximate path lengths of SKS and SKKS in the lowermost mantle, see Figure 6.)



602 **Figure 5.** Shear-wave splitting results for the ScS phase for path ‘C’ (Table 1), for each
 603 slab texture. Each panel shows on the left the fast shear wave orientation in the ray frame (see
 604 Nowacki et al., 2010, Figure 1c), ϕ' , as a black bar located at the ScS core bounce point. Bars
 605 oriented left–right ($\phi' = 90^\circ$) correspond to radial anisotropy with $\xi > 1$, and vertical bars mean
 606 $\xi < 1$ ($\phi' = 0^\circ$), with non-radial anisotropy otherwise (when $0^\circ \neq \phi' \neq 90^\circ$). Colour beneath the
 607 bars is as in Figure 4c. On the right we show the amount of splitting, δt at each bounce point,
 608 coloured by the second scale bar. Crosses signify null measurements. The length of the ray path
 609 of ScS in the lowermost 250 km of the mantle is shown in the right hand panel for the ppv 001
 610 case.

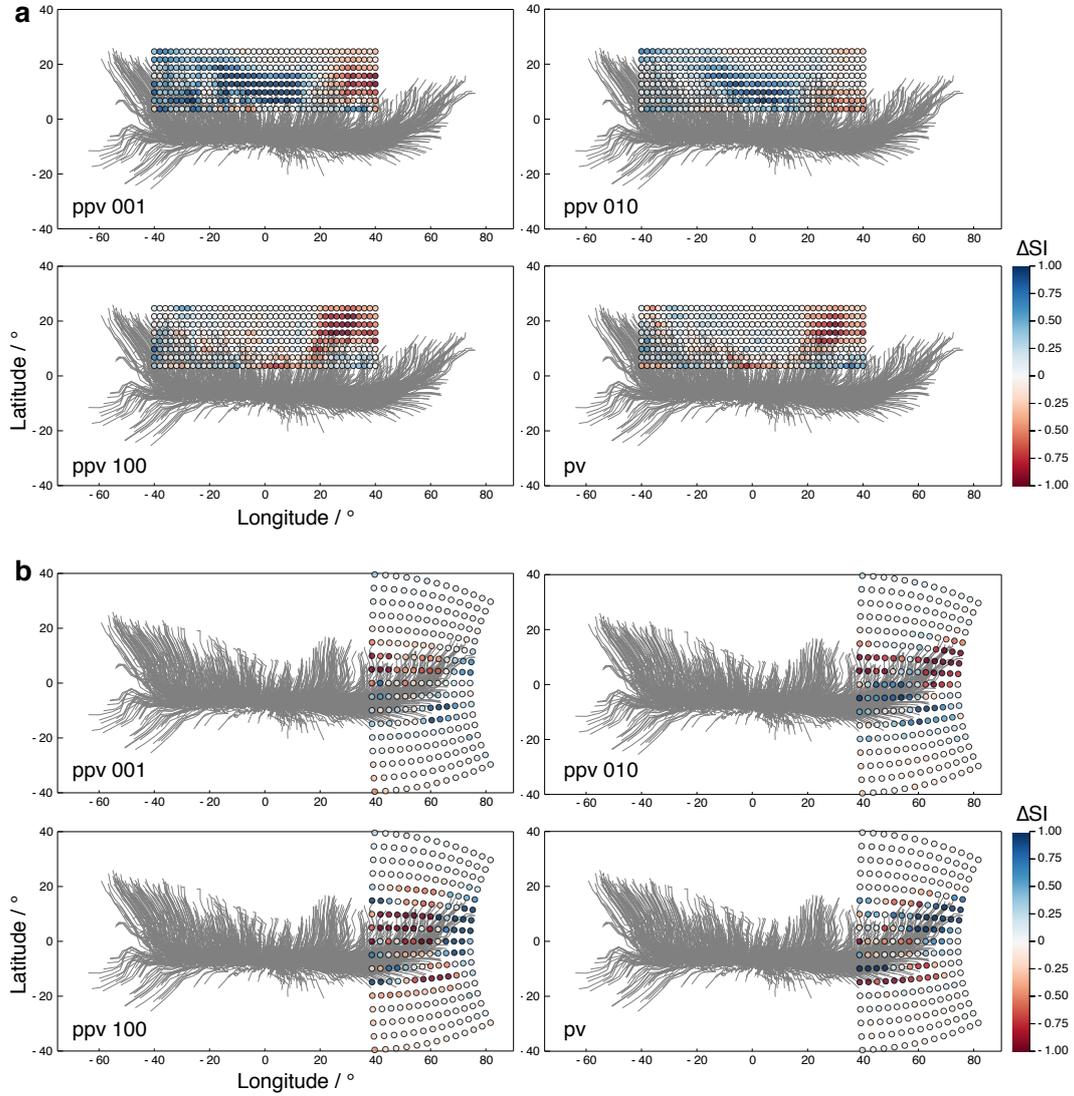


625 **Figure 6.** Shear-wave splitting results for the path ‘B’ (Table 1) and models ppv001 and
 626 ppv010. For each plasticity model, four panels show: (top left) the splitting intensity (Chevrot,
 627 2000) of S_{diff} as colour; (bottom left) the ray-frame fast shear wave orientation of S_{diff} , coloured
 628 by the splitting quality measure Q (Wuestefeld et al., 2010); (bottom right) slow shear-wave
 629 delay time δt , coloured as per the scale bar; and (top right) pairs of discrepant SKS–SKKS
 630 splitting, where the red and orange circles show the core piercing point of SKKS and SKS, re-
 631 spectively, and white circles indicate no discrepant splitting; background colour shows strength
 632 of anisotropy as in Figure 4c. S_{diff} points are plotted at the end of the core-diffracted part of
 633 the path. The lengths of the ray paths of S_{diff} , SKS and SKKS in the lowermost 250 km of the
 634 mantle are shown in the SI panel for the ppv 001 case.



635 **Figure 7.** Shear-wave splitting results for the path 'B' (Table 1) and models ppv100 and pv.

636 Features as for Figure 6.



672 **Figure 8.** Difference in splitting intensity between SKS and SKKS, ΔSI , for (a) path A and
 673 (b) path B (Table 1). ΔSI is shown by colour according to the scale, lower right, at the midpoint
 674 between SKS and SKKS core-mantle boundary piercing points. Grey lines in the background
 675 show the path of tracers particles in the geodynamic model.